

**KWAME NKRUMAH UNIVERSITY OF SCIENCE &
TECHNOLOGY**

INSTITUTE OF DISTANCE LEARNING

DEPARTMENT OF MATHEMATICS



**DETERMINATION OF SHORTEST PATH USING
DIJKSTRA'S ALGORITHM FOR EMERGENCY SERVICE IN
KUMASI METROPOLIS**

BY

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(BSC. MATHEMATICS)

**IN PARTIAL FULFILMENT FOR THE AWARD OF MASTER OF
SCIENCE (INDUSTRIAL MATHEMATICS)**

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KWAME NKRUMAH UNIVERSITY OF SCIENCE & TECHNOLOGY

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METROPOLIS**

**THESIS SUBMITTED TO THE DEPARTMENT OF MATHEMATICS
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BY

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DECLARATION

I hereby declare that this submission is my own work towards the MSc and that, to the best of my knowledge; it contains no material previously published by another person nor material which has been accepted for the award of any other degree of the university, except where due acknowledgement has been made in the text.

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DEDICATION

I DEDICATE THIS TO MY PARENTS

THE LATE MR. MARTIN OBENG AND MADAM DORA NKANSAH



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ABSTRACT

It is becoming difficult for emergence services to find the best route especially in Kumasi to any destination in order to save lives in real time. This study deals with the problem of finding shortest paths in traversing some locations within the Kumasi Metropolis in the

Ashanti Region of Ghana. Dijkstra's Algorithm was selected to determine the shortest distances from any location to any destination within the Kumasi metropolis.

The objective of thesis is to use Dijkstra's algorithm in constructing the minimum spanning tree considering the dual carriage ways in the road network of Kumasi metropolis within the shortest possible time for emergence services. The distance between 51 locations of the towns with the major roads was measured and a legend and a matrix were formulated. A visual basic program was prepared using Dijkstra's algorithm. The distances were used to prepare an input deck for the visual program. The methodology employed included review of relevant literature of the types of Dijkstra's algorithm and methods employed in the solution of the Dijkstra's algorithm and to develop computer solutions – ArcGIS and VB.net for faster computation of Dijkstra's algorithm. The result shows a remarkable reduction in the actual distance as compared with the ordinary routing. These results indicate, clearly the importance of this type of algorithms in the optimization of network flows. Hence the shortest distance from any area in Kumasi metropolis to another can easily be calculated using this thesis so as to minimize the average lost of lives in case emergencies.

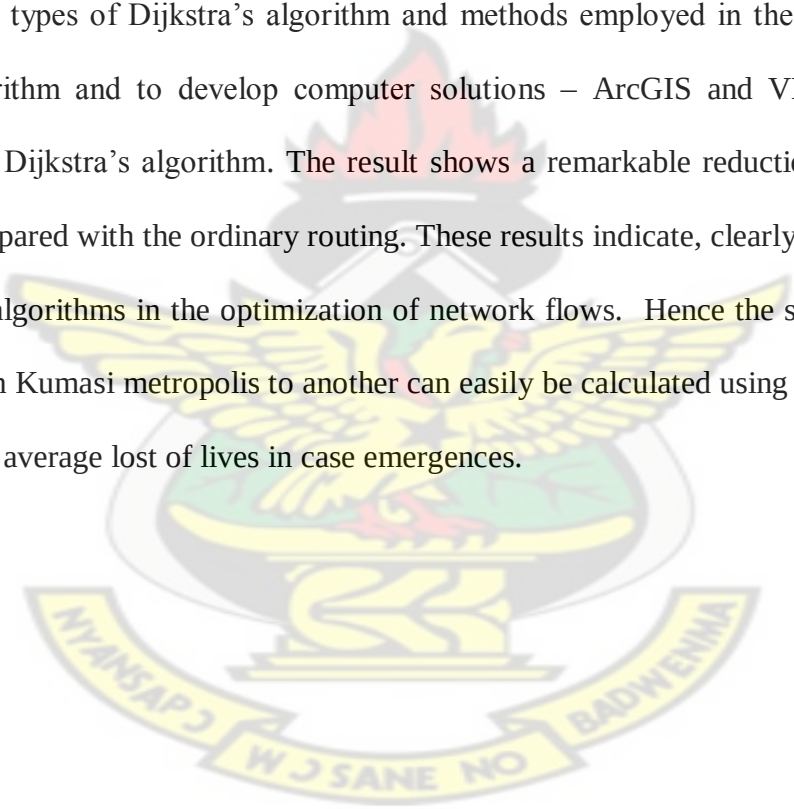


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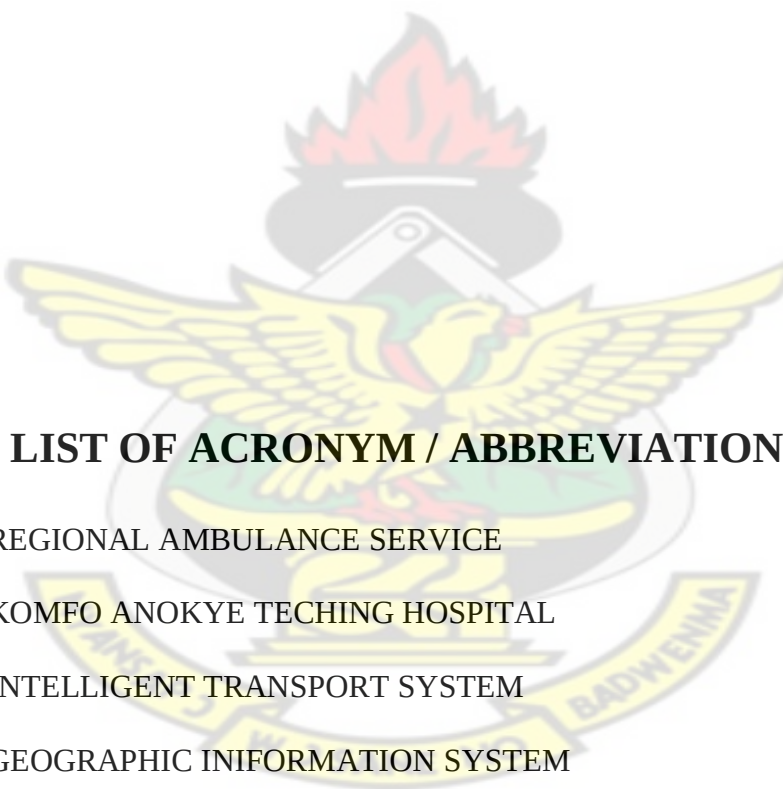
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KNUST



LIST OF ACRONYM / ABBREVIATION

RAS	REGIONAL AMBULANCE SERVICE
KATH	KOMFO ANOKYE TECHING HOSPITAL
ITS	INTELLIGENT TRANSPORT SYSTEM
GIS	GEOGRAPHIC INFORMATION SYSTEM
LBS	LOCATION BASED SERVICE
IVNS	INTELLIGENT VEHICLES NAVIGATION SYSTEM
TMC	TRAFFIC MANAGEMENT CENTRES
GIS-T	GEOGRAPHIC INFORMATION SYSTEMS FOR TRANSPORTATION
NYIA	NEW YOUNG-JONG ISLAND INTERNATIONAL AIRPORT

ESPPRC	ELEMENTARY SHORTEST PATH PROBLEM WITH RESOURCE CONSTRAINTS
VRPTW	VECHICLE ROUTING PROBLEM WITH TIME WINDOWS
SPPRC	SHORTEST PATH PROBLEM WITH RESOURCE CONSTRAINTS
SDSS	SPATIAL DECISION SUPPORT SYSTEM
CARP	CAPACITATED ARC ROUTING PROBLEM
MAS	METROPOLIS AMBULANCE SERVICE
MFS	METROPOLITAN FIRE SERVICE
KMA	KUMASI METROPOLITAN ASSEMBLY



CHAPTER ONE

INTRODUCTION

1.1 BACKGROUND OF THE STUDY

Kumasi is the capital city of the Ashanti Region, a very important and historical centre for Ghana. It is located about 250 km (by road) northwest of Accra. Kumasi is approximately 300 miles north of the equator and 100 miles north of the Gulf of Guinea. It is the second largest city of Ghana with a population of 1,517,000. The metropolis is made up of 119 sub metros. There are five ambulances currently located in Ashanti Region, and one is in the Kumasi metropolis. The one in Kumasi is located at the Komfo Anokye Teaching Hospital (KATH) and the other four ambulances are located at Mampongten, Ejisu, Konongo and Ahwia Nkwanta. All except the KATH and Ahwia Nkwanta services are located at “fire stations”. Cases handled by the Regional Ambulance Service (RAS) range from Gynecology to road accidents. The RAS is housed in a separate building at the KATH polyclinic. The EMTs here run two shifts; day and night. Communication is the key to running of the ambulance service.

1.1.1 DYNAMIC TRAFFIC ROUTING

In recent decades, road transportation systems have become increasingly complex and congested. Traffic congestion is a serious problem that affects people both economically as well as mentally. Moreover, finding an optimal route in an unknown city can be very difficult even with a map. These issues have given rise to the field of Intelligent Transport System (ITS), with the goal of applying and merging advanced technology to make transportation

safer and more efficient by reducing traffic accidents, congestion, air pollution and environmental impact (Ahuja,1993). In working towards this goal, traffic routing is required since the traffic conditions change overtime. Up-to-date, real-time information about traffic conditions can be collected through surveillance systems.

However, the utilization of such information to provide efficient services such as real-time en route guidance still lags behind. The objective of this research is to solve the dynamic routing problem, which guides motor vehicles through the urban road network using the quickest path taking into account the traffic conditions on the roads.

1.1.2 THE ROLE OF GEOGRAPHIC INFORMATION SYSTEMS (GIS) AND LOCATION BASED SERVICE (LBS)

Geographic Information Systems (GIS) represent a new paradigm for the organization and design of information systems, the essential aspect of which is the use of location as the basis for structuring the information systems. Transportation is inherently geographic and therefore the application of GIS has relevance to transportation due to the spatially distributed nature of transportation related data, and the need for various types of network level analysis, statistical analysis and spatial analysis. GIS possesses a technology with considerable potential for achieving dramatic gains in efficiency and productivity for a multitude of traditional transportation applications. The impact of GIS technology in the development of transportation information systems is profound. It completely revolutionizes the decision making process in transportation engineering. This allows the user to understand the logic behind the routing design. With the expansion and proliferation of Location Base Services (LBS) or road map, location awareness and personal location tracking become important attributes of the mobile communication infrastructure and begin to provide invaluable benefits to business, consumer and government sectors. How to establish low-cost, reliable,

and high-quality services is the most important challenge in the LBS area. Navigation is perhaps the most well known function of LBS and Geographic Information Systems for Transportation (GIS-T). It is applied in many land-based transportation applications to revolutionize human lives, such as the Intelligent Vehicles Navigation System (IVNS), which is currently a must-have feature especially in the high-end car market.

1.1.3 THE ARCHITECTURE OF NAVIGATION SERVICE

Navigation guidance can be discriminated between decentralized and centralized route guidance. In the former, drivers derive their own paths using on-board computers, based on either static road maps on paper, or real-time traffic information provided via airwaves (radio) network. However, transportation networks have high costs, limited access, and low connection stability making it expensive to deliver detailed traffic information to all map users. Therefore, it may take a long time to find the destination locally or may even be impossible in some cases. On the other hand, navigation services are often used in time-critical circumstances (e.g. 191 Emergency Service) which require near real-time query response and concise route guidance information to facilitate decision making.

Centralized route guidance relies on Traffic Management Centres (TMC) such as some FM stations to answer path queries submitted by drivers. In this case, the Client/Server architecture is employed in order to reduce query response time. A centralized GIS server is used to perform the geo-processing task and return query results instead of providing the entire dataset. The service can provide users turn-by-turn navigation instructions about optimal routes to their desired destinations through text or a map display. It can also alert the driver about problems ahead, such as traffic jams or accidents. To deliver query results to mobile clients within a tolerable latency time, it demands an efficient algorithm to retrieve desired navigation information quickly. Thus, it is able to accommodate large numbers of

road users. This thesis, discusses the algorithms that are feasible for centralized route guidance.

1.2 STATEMENT OF THE PROBLEM

Travelling is a part of daily life. The majority of people (especially in large cities or developing countries) rely heavily on emergencies services in the case of accident such as road accident, fire and any disaster event people will rely on these emergence services instead of their own vehicles. In a metropolis with a complicated transport network, people often do not know how to reach their destination except where they often visit. In addition, people may want to plan for the fastest or the most economical method to their destinations. Such tasks require a sophisticated knowledge about public transport network. Further, we need a multi-modal route finding system, because a transport network comprises many modes of transportation, including railway, bus, mini-bus, and so on, within a large metropolis such as Kumasi. When a user asks for a path from one place to another, the system can generate routes, in multi-modal or single modal mode, according to input criteria, such as cost, time, or transportation mode.

Transportation model is but one of the many problems that can be represented and solved as a network problem. To be specific consider the following situations:

- (i). Determination of the minimum- cost flow schedule from oil fields to refineries and finally to distribution centre this can be transported through tracks, trains etc.
- (ii). Determination of the shortest route joining two cities in an existing network of roads.
- (iii). Collection, transporting and dumping of garbage.
- (iv). Business, scheduling deliveries and installations while including time window restrictions, or a calculating drive time to determine customer base, taking into account rush hour versus midday traffic volumes.

- (v). Education, generating school bus routes honouring curb approach and no U-turn rules.
- (vi). Environmental Health, determining effective routes for county health inspectors.
- (vii). Public Safety, routing emergency response crews to incidents, or calculating drive time for first responder planning.
- (viii). Public Works, determining the optimal route for point-to-point pickups of massive trash items or routing of repair crews.
- (ix). Retail, finding the closest store based on a customer's location including the ability to return the closest ranked by distance.
- (x). Transportation, calculating accessibility for mass transit systems by using a complex network data set.

A study of this representative list reviews that;

Situation a) is a minimal spanning tree model

Situation b) is a shortest route model

Situation c) is a minimum-cost capacitated network model

The examples cited above deal with the determination of distances and material flow in a literal sense, the network models listed can be represented, and in principle, solve as linear programs. However the tremendous number of variables and constraints that normally accompanies a typical network model makes it inadvisable to solve network problems directly by the simplex method. The nature and/or structure of these problems allow the development of highly efficient algorithms, which in most cases are based on linear programming theory.

1.3 OBJECTIVES OF THE STUDY

The objective of this thesis is to create a formation movement shortest path finding algorithm for emergencies services vehicles to implement tactical movement within a large metropolis such as Kumasi and optimization scheme for transportation planning and analysis to provide a major advantage in its ability to take into account a range of different, often unrelated criteria, even if these criteria cannot be directly related to quantitative outcome measures.

1.4 METHODOLOGY

Generally, methodology consists of the study major routes, sampling procedure, sample size and how the data is analyzed. Kumasi Metropolis, however, has been selected as the reference region. The methodology employed included review of relevant literature of the types of Dijkstra's algorithm and methods employed in the solution of the Dijkstra's algorithm and to develop computer solutions – ArcGIS and VB.net for faster computation of Dijkstra's algorithm.

1.5 JUSTIFICATION

With the development of geographic information systems (GIS) technology, network and transportation analyses within a GIS environment have become a common practice in many application areas. A key problem in network and transportation analyses is the computation of shortest paths between different locations on a network. Sometimes this computation has to be done in real time. For the sake of illustration, let us have a look at the case of a 911 call requesting an ambulance to rush a patient to a hospital. Today it is possible to determine the fastest route and dispatch an ambulance with the assistance of GIS. Because a link on a real road network in a city tends to possess different levels of congestion during different time periods of a day, and because a patient's location cannot be expected to be known in advance,

it is practically impossible to determine the fastest route before a 191 call is received. Hence, the fastest route can only be determined in real time. In some cases the fastest route has to be determined in a few seconds in order to ensure the safety of a patient. Moreover, when large real road networks are involved in an application, the determination of shortest paths on a large network can be computationally very intensive. Because many applications involve real road networks and because the computation of a fastest route (shortest path) requires an answer in real time, a natural question to ask is: Which shortest path algorithm runs fastest on real road networks? Although considerable empirical studies on the performance of shortest path algorithms have been reported in the literature (Dijkstra 1959; Dial et al., 1979; Glover et al., 1985; Gallo and Pallottino 1988; Hung and Divoky 1988; Ahuja et al., 1990; Mondou et al., 1991; Cherkassky et al., 1993; Goldberg and Radzik 1993), there is no clear answer as to which algorithm, or a set of algorithms runs fastest on real road networks. In a recent study conducted by Zhan and Noon (1996), a set of three shortest path algorithms that run fastest on real road networks has been identified. These three algorithms are:

- (i). the graph growth algorithm implemented with two queues,
- (ii). the Dijkstra's algorithm implemented with approximate buckets, and
- (iii). the Dijkstra's algorithm implemented with double buckets.

Dijkstra's algorithm was then used on the node graph, but modified to run faster using this extra data. However this optimization changes Dijkstra's Algorithm so that it only finds a path, rather than the shortest path. Other applications of Dijkstra are

- (i). Routing of postal workers
- (ii). Routing robots through a warehouse
- (iii). Drilling holes on printed circuit board

A network consists of a set of points and a set of lines connecting certain pair of the points. These points are called nodes and are linked by arcs, edges or branches. Associated with each

arc is the flow of some type. In a transportation network, cities represent nodes and highways represent edges or arc, with traffic representing arc flow. The standard notation for describing network $G = (N, A)$ where N is the set of nodes and A is the set of edges or arcs.

Today it is possible to determine the faster route and dispatch the immediate assistance or with the help of the assistance of Geological Information System {G.I.S). With the advance development in technology, the analyses of networking and transportation within the technological environment have become a common practice in many applicable areas. The key problem in network and transportation is the computation of the SHORTEST PATHS between different locations on a network Sometimes this computation has to be done in real times. For the sake of illustration, let us have a look at the case of an emergency call, requesting an ambulance to rush a patient from a very remote area to a hospital. Because a link on a real road network in the city tends to posse different levels of congestion during different time period of a day and because a Patient's location cannot be expected to be known in advance, it is practically impossible to determine the fastest route before a call is received. Hence the fastest route can only be determined in real time.

In some cases the fastest route has to be determined in a few second in order to ensure the safety of a patient. Moreover when large real road network are involved in an application, the determination of SHORTEST PATHS on a large network can be computationally very intensively. The collection, transport and disposal of solid waste, which is a highly visible and important municipal service, involves a large expenditure but receives, scant attention.

This problem is even more crucial for large cities in developing countries due to the hot weather. A constructive heuristic, which takes into account the environmental aspect as well as the cost, is proposed to solve the routing aspect of garbage collection. This is based on a look-ahead strategy, which is enhanced by this additional mechanism:

The problem and its impact on the environment collection of household refuse/industrial waste is one of the most difficult operational problems faced by local authorities in any large city. The collection problem is especially crucial for cities in developing countries. Solid wastes generated from urban and industrial sources also contain a large number of ingredients, some of which are toxic.

1.6 LIMITATIONS

Among several variants of the SP algorithms there is a group of algorithms, which could be applied to solve the present issue, but the solution would not be efficient. An obvious group of algorithms is the one that gives a more general solution than needed and their solution would be redundant. A good example of a group giving a redundant solution is the ‘all pairs’ group of the SP algorithms: only one pair of nodes would be used from the set of all pairs.

Matrix algorithms are not of a good use for sparse networks. Matrix algorithms are memory consuming and for sparse networks time consuming. The implementation of the Dijkstra’s algorithm based on a matrix is inefficient for road networks. Therefore the matrix algorithms are abandoned from this point for the rest of the report.

Determining the “best” route or set of routes for linear utilities such as highways, pipelines, and power transmission lines, through a landscape has been the subject of much research in geographic information systems (GIS) and spatial decision making. Specifying an optimal corridor that connects an origin and destination is analogous to identifying a least-cost-path through a varying space. Extensive research efforts have been executed to solve the problems for many years (Tomlin, 1990; Eastman, 1989; Douglas, 1994; Berry 2004). Tomlin’s (1990) Spread algorithm generates an accumulated-cost-surface iteratively and delineates the weighted shortest path from any location to a destination by tracing back along slope lines. Eastman (1989) implemented a similar, but more efficient, push broom algorithm, which is able to produce an accumulated cost surface within three iterations. Many of the existing

least-cost-path algorithms in GIS are derived from the Dijkstra's shortest path algorithm and intend to generate a global optimal solution.

1.7 ORGANIZATION OF THE THESIS

The thesis is organized in five chapters

Chapter one consists of the introduction to the shortest path and the use of Dijkstra's over other shortest path algorithm. The background, problem statement, objective, methodology, justification and the limitations are discussed. In chapter two we shall put forward pertinent literature in field of shortest path algorithm and its application. Chapter three presents and gives a detailed explanation of the shortest path algorithm with Dijkstra's algorithms in detailed. Chapter four consist of the data collection, analysis and results. Chapter five, which is final chapter, focus on conclusion and recommendations.



CHAPTER TWO

LITERATURE REVIEW

2.1 INTRODUCTION

Shortest path problems are the most fundamental and the most commonly encountered problems in the study of transportation and communication networks (Syslo 1983).

There are many types of shortest path problems. For example, we may be interested in deterring the shortest path (i.e the most economic path or fastest path or minimum – fuel consumption path) from one specified node in the network to another specified node; or may need to find shortest paths from a specified node to all other nodes.

Arrival time dependent shortest path finding is an important function in the field of traffic information systems or telematics. However, large number of mobile objects on the road network results in a scalability problem for frequently updating and handling their real-time location. Kim (2005) proposed a query processing method in MANET (Mobile Ad-hoc Network) environment to find an arrival time dependent shortest path with a consideration of both traffic flow and location in real time. Since their traffic flow method does not need a centralized server, time dependent shortest path query is processed by in-network way. In order to reduce the number of messages to forward and nodes to relay, the control introduce an on-road routing, where messages are forwarded to neighbouring nodes on the same or adjacent road segments. This routing method allows the collection of traffic information in real time and the reduction of the number of routing messages.

Experiments show that the number of forwarded messages is reduced in an order of magnitude with our on-road routing method compared to LAR-like method. At best, our method reduces about fifty seven (57) times less messages.

The Integrated Transport Information System (ITIS) project for the Klang Valley was initiated by the Federal Government in early 2001 and deployed on a design – build basis in 3Q 2002. With the City Hall, Kuala Lumpur as the implementing agency, the project was successfully completed and handed over in June 2005. Using a spectrum of different technologies and equipment, the ITIS has since been gainfully used by City Hall as well as the police for management of road network operations and particular for management of incidents over a network comprising of over 200kms of roadways. Omar (1994) discussed the technologies used in the ITIS network operations, in particular in the detection and management of incidents, lesson learnt – to – date as well as the roadmap for future operations and ITS related deployment. Optimization of forest road network is an important part of logging planning. Matthews (1942) was first to introduce a method for optimization of road spacing based on minimization of road and skidding cost. Ghaffarian (2000), found the best road network for a district harvested by skidder. The skidding model developed by stepwise regression model was used to predict the cost skidding per cubic meter for the thirty nine (39) nodes, which were planned in the district map.

The harvesting volume and road cost per each node were computed. The data were entered into network 2000 and the shortest path algorithm; simulated annealing and great deluge algorithms were run to find the best solution to optimise logging cost of the district. The result showed which roads can be eliminated from the existing forest road network. Due to the reduction of travel time between regions in recent years by the development of transportation networks in Japan, the opportunities for anyone living in both urban and rural areas to meet people and to use urban facilities have increased. However, the various functions of smaller cities will be absorbed into these larger metropolises, since the sphere of

urban influence from big cities spreads to greater areas. In these backgrounds, the impacts of developments of expressway networks are analyzed by using the increment in interchangeable population and the changes in trade and recreation areas. Problems rural cities will have to bear in the near future are also discussed. It can be said that one result of this is the sphere of urban influence from big cities will spread to the retailing industry in rural areas in the near future. In order to utilize the expressway improvements effectively in rural cities, new and creative development policies are required which are dissimilar to those of major cities (Hirose, 1994).

Setoguchi et al., (1994) analyzed the influence of network extension and the revised toll on the traffic of urban expressways in Fukuoka, Kita-Kyushu, and Nagoya, and, in estimating the traffic of these urban expressways, based on their maintenance and management, the author of this paper straightened out the relationships between the toll, a factor that determines the conversion amount of traffic, and the value of time to examine what traffic allocation calculations should be at a practical application level. Hiroshi et al., (1994) proposed to determine the groups of road sections to be simultaneously constructed and the priority between them, considering the disutility of road construction and the priority and simultaneity of construction between road sections. Dynamic programming is utilized for an optimization procedure. The mathematical modelling of the problem and its solution technique are emphasized. An example problem is included and illustrated for showing the applicability of the model. The results indicate that the proposed method is useful for multi-stage determination problem such as in the road network planning. Talib et al., (1994) described a method, which determines a plan for improving a road network taking into consideration the impact of increasing number of trip generation.

In this method, the increasing number of trip generation in study area is distributed to other unfurnished residential zones, and the groups of road segments to be simultaneously constructed as well as their priority are determined so that the limited budget will be

effectively used. The dynamic programming is utilized for the optimization procedure. In the recent years, with the development of social economy in China, the public urban transportation has greatly changed. In Beijing city, taxi traffic system has become a new kind of public transit means for resident trips. Takeshi et al., (1994) first introduced the development history of taxi traffic system of Beijing city, which includes three stages of taxi service trades from original to now. Through the introduction, the historical reasons that taxi traffic development of Beijing city is increasingly expanding can be known. The second part analyses the interior and exterior circumstances and impact factors of taxi traffic system, and describes the improvement of relative traffic installation and the change of transportation policy of Beijing city. Further, they preliminarily study the developing strategies of Beijing taxi traffic system through the discussion on the change of passenger flow and the estimation of corresponding factors, and comparison with other big cities such as Taipei, Mexico city etc. The new Young-Jong island international airport (NYIA) and the related hinder land development is expected to be a catalyser, which stimulates even further Korea's economic power and participation of a global market. The basis of the development plan is characterized by following aspects: backup for the Northeast Asian hub due to the globalization trends, urgency of the social overhead capital building, rapid increasing of aviation demand and shortage of the existing facilities. According to this basis, the plan includes international business centre, community development and free trade zone. The main impacts of NYIA plan can be separated into the reinforcement of international competitiveness, the boosting of regional development and the opening of a window on cultural exchange. Also, it is necessary to participate the private sectors and to control different opinions within various government departments (Lee , 1994). Chikashi et al., (1994) described the characteristics of traffic behaviours such as traffic purposes at holidays and week days, selection of transportation modes, walking and selection of parking place to the central area of a local city. Data are obtained from response to questionnaires for people

in Miyazaki City. The choice behaviour of parking places is analyzed by using Aggregated Logit Model. The analyses results and answers show that it is necessary to decrease the traffic resistance on walking by such method as pedestrian and vehicular segmentation to keep traffic safe for pedestrian.

Aminu, (2007) put forward the problem of finding shortest paths in traversing some location within the Sokoto Metropolis. In particular, it explores the use of Dijkstra's algorithm in constructing the minimum spanning tree considering the dual carriage ways in some of the road in Kumasi Metropolis. The results shows that a reduction in the actual distance as compared with ordinary routing. These results indicate, clearly the importance of this type of algorithms in the optimisation of network flows. Lehr- und Forschungsgebiet Operations Research und Logistik Management (RWTH) Aachen, Templergraben 64, 52056 Aachen, Germany The elementary shortest path problem with resource constraints (ESPPRC) is a widely used modelling tool in formulating vehicle routing and crew scheduling applications. The ESPPRC consists of finding shortest paths from a source to all other nodes of a network that do not contain any cycles, i.e. duplicate nodes. The ESPPRC occurs as a sub problem of an enclosing problem and is used to implicitly generate the set of all feasible routes or schedules, as in the column generation formulation of the vehicle routing problem with time windows (VRPTW). The ESPPRC problem being NP-hard in the strong sense, classical solution approaches are based on the corresponding non-elementary shortest path problem with resource constraints (SPPRC), which can be solved using a pseudo-polynomial labelling algorithm. While solving the enclosing master problem by branch-and-price, this sub problem relaxation leads to weak lower bounds and sometimes impractically large branch-and-bound trees. A compromise between solving ESPPRC and SPPRC is to forbid cycles of small lengths. In the SPPRC with k-cycle elimination (SPPRC-k-cyc) only paths with cycles of length at least $(k + 1)$ are allowed. The case $k = 2$ which forbids sequences of the form i to $(j - i)$ is well known, and has been used successfully to reduce integrality gaps for the VRPTW

propose a new definition of the dominance rule among labels for dealing with arbitrary values of $k \geq 2$. The numerical experiments on the linear relaxation of some hard VRPTW instances from Solomon's benchmark set show that k -cycle elimination with $k \geq 3$ can substantially improve the lower bounds. Using well-known techniques for branching and cutting, the new algorithm has proven to be a key ingredient for getting exact integer solutions of knowingly hard problems from the literature. Eklund, et al., (1994) discussed the implementation of Dijkstra's classic double bucket algorithm for path finding in connected networks.

The work reports on a modification of the algorithm embracing both static and dynamic heuristic components and multiple source nodes. The modified algorithm is applied in 3D Spatial Information System (SIS) for routing emergency service vehicles. The algorithm has been implemented as a suite of modules and integrated into a commercial SIS software environment. Genuine 3Dspatial data is used to test the algorithm on the problem of vehicle routing and rerouting under simulated earthquake conditions in the Japanese city of Okayama. Coverage graphs were also produced giving contour lines joining points with identical travel times. Shortest Path problems are inevitable in road network applications such as city emergency handling and drive guiding system, in situations where the optimal routings have to be found. As the traffic condition among a city changes from time to time and there are usually huge amounts of requests that occur at any moment, needs to quickly find the solution. Therefore, the efficiency of the algorithm is very important. Some approaches take advantage of pre-processing that compute results before demanding.

These results are saved in memory and could be used directly when a new request comes up. This can be inapplicable if the devices have limited memory and external storage. Liang (2005) aimed only at investigating the single source shortest path problems and intended to obtain some general conclusions by examining three approaches: Dijkstra's shortest path algorithm, Restricted search algorithm and A*algorithm. To verify the three algorithms, a program was developed under Microsoft Visual Basic .Net environment. The three

algorithms were implemented and visually demonstrated. The road network example is a graph data file containing partial transportation data of the Ottawa city.

Since the aftermath of typhoon Herb in 1996, all sort of flood and drought followed in 2002 have claimed lives and countless property, which have imposed serious economic damage on the country. The collection of flood information is the basis for established prevention system. It is anticipated that flood information management system will include flood insurance, flood warning, damage notification and incorporation with GIS in the future to provide further capabilities. The use of the ArcGIS and mathematical programming, in accordance to the properties of the disaster, aims pragmatically at a balance between the reliefs of a disaster and the shortest time for conveying the equipments, and to construct the optimal model of the equipment's transportation and mobilisation of the emergency. The system could trace and manage more efficiently, the equipments in urgent need of repair, and reconstruct the state of the recovery.

Humblet (1988) employed a distributed algorithm to compute shortest paths in a network with changing topology. It does not suffer from the routing table looping behaviour associated with the Ford-Bellman t-distributed shortest path algorithm although it uses truly distributed processing. Its time and message complexities are evaluated.

Saunders and Takaoka presented new algorithms for computing shortest paths in a nearly acyclic directed graph $G = (V, E)$. The new algorithms improve on the worst-case running time of previous algorithms. Such algorithms use the concept of a 1-dominator set.

A 1-dominator set divides a graph into a unique collection of acyclic sub graphs, where each acyclic sub graph is dominated by a single associated trigger vertex. The previous time for computing a 1- dominator set is improved from $O(mn)$ to $O(m)$, where $m = |E|$ and $n = |V|$. Efficient shortest path algorithms only spend delete-min operations on trigger vertices, thereby making the computation of shortest paths through nontrigger vertices easier. Under this framework, the time complexity for the all-pairs shortest path (APSP) problem is

improved from $O(mn + nr \log r)$ to $O(mn + r^2 \log r)$, where r is the number of triggers. Here the second term in the complexity results from delete-min operations in a heap of size r . The time complexity of the APSP problem on the broader class of nearly acyclic graphs, where trigger vertices correspond to any precomputed feedback vertex set, is similarly improved from $O(mn + nr^2)$ to $O(mn + r^3)$. The paper also mentioned that the 1-dominator set concept can be generalised to define a bidirectional 1-dominator set and k -dominator sets. When you drive to somewhere ‘far away’, you will leave your current location via one of only a few ‘important’ traffic junctions. Starting from this informal observation, develop an algorithmic approach—transit node routing—that allows us to reduce quickest-path queries in road networks to a small number of table lookups. Present two implementations of this idea, one based on a simple grid data structure and one based on highway hierarchies. For the road map of the United States, our best query times improve over the best previously published figures by two orders of magnitude. Our results exhibit various trade-offs between average query time (5 μ s to 63 μ s), preprocessing time (59 min to 1200 min), and storage overhead (21 bytes/node to 244 bytes/node) Bast et al., (2006). On the basis of analyzing the advantages and disadvantages of the shortest path algorithm and the problem solving based on knowledge method, it is clearly showed that neither the algorithm, which provides the precise solution nor the common method, which is totally suitable to people’s usual finding activities and based on the common sense, can provide us with a satisfactory solution. However, they can be complementary to each other, and this has made the combined use of the two to become a necessity. Rong, WENG Min, DU QingYun, and CAI ZhongLiang put forward the combination use of knowledge and algorithm for way-finding. In this combined method, the knowledge is used for retrieving the case and isolating the searching area while algorithm is used for finding out the best solution in the isolated areas. The study shows that although the new approach cannot always ensure a most accurate solution, it not only prunes off a lot of search space but also produces routes that meet people’s preference of travelling on familiar

and major roads. Yu et al., (1995) proposed a hierarchical algorithm for approximating all pairs of shortest paths in a large scale network. The algorithm begins by extracting a high level sub network of relatively long links (and their associated nodes) where routing decisions are most crucial. This high level network partitions the shorter links and their nodes into a set of lower level sub networks. By fixing gateway nodes within the high level network for entering and exiting these sub networks, a computational savings is achieved at the expense of optimality. They explore the magnitude of this trade off between computational savings and associated error both analytically and empirically with a case study of the South-eastern Michigan traffic network. An order of magnitude drop in computational times was achieved with an on – line route guidance simulation at the expense of a five percent (5%) increase in expected trip times. A lot of the related work on shortest paths in stochastic networks has focused on the notion of shortest paths in expectation, e.g., (Bertsekas and Tsitsiklis 1991). Other models have added costs on the edges in addition to travel times (Chabini 2002), (Miller-Hooks and Mahmassani 2000) where the costs depend on the realized travel times and in this way can capture a measure of uncertainty.

Finding the path of smallest expected length trivially reduces to deterministic shortest path problems and does not take into account risk in predicting the optimal route. Since most real world applications care about a trade off between risk and expectation, we consider nonlinear objectives that capture more information about the edge distributions. Closest to this model, Loui (Loui, 1983) considered a decision analytic framework for optimal paths under uncertainty, however, he only studied monotone increasing cost functions and his algorithm has running time $O(n^2)$ in the worst case. Mirchandani and Soroush (Mirchandani and Soroush, 1985) extended his work to a quadratic cost function of the path length, however their algorithm is also an exhaustive search over all potentially optimal paths, and thus exponential in the worst case.

Another branch of the stochastic shortest path literature has focused on adaptive algorithms (Fan, Kalaba and Moore 2000), (Gao and Chabini, 2002), (Boyan and Mitzenmacher, 2001), which compute the optimal next edge in light of lengths or travel times already realized en route to the current node. Another direction has been to give approximations and heuristics for expected shortest paths in stochastic networks with nonstationary (time-varying) edge length distributions (Miller-Hooks and Mahmassani, 2000), (Fu and Rilett, 1998), (Hall, 1986), to list a few. In this proposal, we only consider stationary edge length distributions that do not change with time; time-varying distributions will be the subject of future work.

Delava et al., (2008) show that accomplishing an effective routing of emergency vehicle will minimize its response time and will thus improve the response performance. Traffic congestion is a critical problem in urban area that influences the travel time of vehicles. The aim of this study is developing a spatial decision support system (SDSS) for emergency vehicle routing. The proposed system is based on integration of geospatial information system (GIS) and real-time traffic conditions. In this system dynamic shortest path is used for emergency vehicle routing. This study investigates the dynamic shortest path algorithms and offers an applicable solution for emergency routing. The shortest path applied is based on the Dijkstra algorithm in which specific rules have been used to intelligently update the proposed path during driving. Results of this study, illustrate that dynamic vehicle routing is an efficient solution for the reduction of travel time in emergency routing. Finally, it is shown that using GIS in emergency routing offers a powerful capability for network analysis, visualization and management of urban traffic network. Spatial analysis capabilities of GIS are used to find the shortest or fastest route through a network. These capabilities of GIS for analyzing spatial networks enable them to be used as decision support systems (DSSs) for dispatching and routing of emergency vehicles. In agent based traffic simulations which use systematic relaxation to reach a steady state of the Scenario, the performance of the routing algorithm used for finding a path from a start node to an end node in the network is crucial

for the overall performance. For example, a systematic relaxation process for a large scale scenario with about 7.5 million inhabitants (roughly the population of Switzerland) performing approximately three trips per day on average requires about 2.25 million route calculations, assuming that 10% of the trips are adapted per iteration. Expecting about 100 iterations to reach a stable state, 225 million routes have to be delivered in total. Lefebvre and Balmer (2008) focus on routing algorithms and acceleration methods for point-to-point shortest path computations in directed graphs that are time-dependent, i.e. link weights vary during time. The work is done using MATSim-T (Multi-Agent Traffic Simulation Toolkit) which is used for large-scale agent-based traffic simulations. The algorithms under investigation are both variations of Dijkstra's algorithm and the A*-algorithm. Extensive performance tests are conducted on different traffic networks of Switzerland. The fastest algorithm is the A*-algorithm with an enhanced heuristic estimate: While it is up to 400 times faster than Dijkstra's original algorithm on short routes, the speed compared to Dijkstra's diminishes with the length of the route to be calculated. The waste collection problem can also be modelled as the Capacitated Arc Routing Problem (CARP). As this problem cannot be solved by optimal (exact) methods in practice, heuristics are used for this purpose. One possible approach is first to find a giant tour and then decompose it into a set of routes that are feasible with regard to the vehicle capacity.

More importantly in the inspection of distributed systems such as electric poles, gas pipeline telephone line and a whole lot more so as faults to be rectify as soon as possible. Because many applications involves real networks and also because the computation of a fastest route (shortest path) requires an answer in real time a natural question to ask is which shortest path runs fastest on real road networks?

Although there are a number of shortest path algorithms such as:

Dijkstra's

Floyd's

Glover et al Goldberg and Radzik etc.

But there is no clear answer as to which algorithm, or a set of algorithms runs faster on a real road network.

KNUST



CHAPTER THREE

METHODOLOGY

3.0 METHODOLOGY

The methodology employed included review of relevant literature of the types of Dijkstra algorithm and methods employed in the solution of the Dijkstra algorithm and to develop computer solutions – ArcGIS and VB.net for faster computation of Dijkstra algorithm

3.1 BACKGROUND OF GRAPH THEORY

In this chapter, some fundamental concepts of graph theory are introduced and will be referred to in subsequent discussions.

3.2 DEFINITION OF A GRAPH

In mathematics and computer science, graph theory deals with the properties of graphs. Informally, a graph is a set of objects, known as nodes or vertices, connected by links, known as edges or arcs, which can be undirected or directed (assigned a direction). It is often depicted as a set of points (nodes, vertices) joined by links (the edges). Precisely, a graph is a pair, $G = (V; E)$, of sets satisfying $E \subseteq [V]$; thus, the elements of E are 2-element subsets of V . The elements of V are the nodes (or vertices) of the graph G , the elements of E are its links (or edges). In this case, E is a subset of the cross product $V * V$ which is denoted by $E \subseteq [V]$. To avoid notational ambiguities, we shall always assume that $V \cap E = \emptyset$.

A connected graph is a non-empty graph G with paths from all nodes to all other nodes in the graph. The order of a graph G is determined by the number of nodes. Graphs are finite or infinite according to their order. In this thesis, the graphs are all finite and connected. Furthermore, a graph having a weight, or number, associated with each link is called a weighted graph, denoted by $G = (V; E; W)$. An example of a weighted graph is shown in

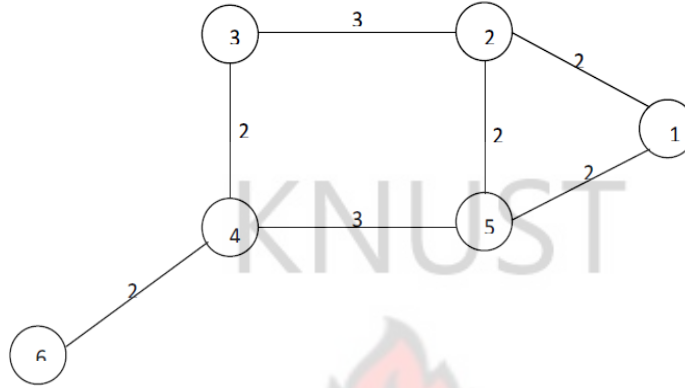


Figure 3.1: A diagram of a weighted graph with 6 nodes and 7 links.

3.2.1 DEGREE OF A VERTEX (NODE)

A node v is incident with a link e if $v \in e$; then e is a link at v . The two nodes incident with a link are its end nodes. The set of neighbours of a node v in G is denoted by $N(v)$. The degree $d(v)$ of a node v is the number $|E(v)|$ of links incident on v . This is equal to the number of neighbours of v . A node of degree 0 is isolated. The number $\delta(G) = \min \{d(v) \mid v \in V\}$ is the minimum degree of G , while the number $\Delta(G) = \max \{d(v) \mid v \in V\}$ is the maximum degree. The average degree of G is given by the number

$$d(G) = \frac{1}{|V|} \sum_{v \in V} d(v) \quad (3.2)$$

Clearly,

$$\delta(G) \leq d(G) \leq \Delta(G)$$

The average degree globally quantifies what is measured locally by the node degrees: the number of links of G per node. Sometimes it is convenient to express this ratio directly, as $\epsilon(G) = |E|/|V|$. The quantities d and ϵ are intimately related. Indeed, if we sum up all of the node degrees in G , we count every link exactly twice: once from each of its ends.

Thus,

$$|E| = \frac{1}{2} \sum_{v \in V} d(v) = \frac{1}{2} d(G) \cdot |V| \quad 3.3$$

and therefore

$$\varepsilon(G) = \frac{1}{2} d(G) \quad 3.4$$

Graphs with a number of links that are roughly quadratic in their order are usually called dense graphs. Graphs with a number of links that are approximately linear in their order are called sparse graphs. Obviously, the average degree $d(G)$ for a dense graph will be much greater than that of a sparse graph.

In a graph, a path, from a source node s to a destination node d , is defined as a sequence of nodes $(v_0, v_1, v_2, \dots, v_k)$ where $s = v_0$, $d = v_k$, and the links $(v_0, v_1), (v_1, v_2), \dots, (v_{k-1}, v_k)$ are present in E . The cardinality of a path is determined by the number of links. The cost of a path is the sum of the link costs that make up the path.

An optimal path from node u to node v is the path with minimum cost, denoted by (u, v) . The cost can take many forms including travel time, travel distance, or total toll. In my research, the cost or weight of a path stands for the travel time which is needed to go through the path.

3.2.2 TRANSPORTATION NETWORK DATA MODEL

A transportation network is a type of directed, weighted graph. The use of GIS for transportation applications is widespread and a fundamental requirement for most transportation GIS is a structured road network. In developing a transportation network model, the street system is represented by a series of nodes and links with associated weights. This representation is an attempt to quantify the street system for use in a mathematical model. Inherent in the modeling effort is a simplification of the actual street system. The network nodes represent the intersections within the street system and the network links represent the streets. The weights represent travel time between the nodes.

As a specialized type of graph, a transportation network has characteristics that differ from the general graph. A suitable data structure is required to represent the transportation network. Comparing the three data structures, an adjacency list representation of the graph occupies less space because it does not require space to represent links which are not present. The space complexity of an adjacency list is $O(|E| + |V|)$, where $|E|$ and $|V|$ are the number of links and nodes respectively. In contrast, incidence matrix and adjacency matrix representations contain too many 0s which are useless and redundant in storage. The space

complexity of incidence matrices and adjacency matrices are $O(|E| \times |V|)$ and $O(|V|^2)$ respectively. In the following discussion, we shall take a more detailed look at the three data models in terms of storage space and suitable operations. Using a naive linked list implementation on a 32-bit computer, an adjacency list for an undirected graph requires approximately $16 \times (|E| + |V|)$ bytes of storage space. On the other hand, because each entry in the adjacency matrix requires only one bit, they can be represented in a very compact way, occupying only $|V|^2 / 8$ bytes of contiguous space. First, we assume that the adjacency list occupies more memory space than that of an adjacency matrix. Then

$$16 \times (|E| + |V|) \geq \frac{|V|^2}{8}$$

Based on equation (3.1.2) in section 3.1, we have,

$$16 \times \left(\frac{1}{2} d(G) \times (|V| + |V|)\right) \geq \frac{|V|^2}{8}$$

where $d(G)$ is the average degree of G .

$$d(G) \geq \frac{|V| - 128}{64} \quad 3.5$$

This means that the adjacency list representation occupies more space when equation (3.5) holds. In reality, most transportation networks are large scale sparse graphs with many nodes but relatively few links as compared with the maximum number possible ($|V| \times (|V| - 1)$ for maximum). That is, there are no more than 5 links ($\Delta(G) \approx 5$) connected to each node. In most cases there are usually 2, 3 or 4 ($\delta(G) = 2$) links, although the maximum links is $|V| - 1$ for each node. Also, road networks often have regular network structures and a normal layout, especially for well planned modern cities. Again most transportation networks are near connected graphs, in which any pair of points is traversable through a route. Assuming the average degree of a road network is 5, equation 3.5 holds only if $|V| \leq 448$.

However, most road networks contains thousands of nodes where $|V| \gg 448$. As a result, equation 3.2 cannot hold. Thus, the adjacency list representation occupies less storage space than that of an adjacency matrix. For example, consider a road network containing 10000 nodes. If an adjacency matrix is employed to store the network, at least 10 megabytes of memory space is required. It will most likely take more computational power and time to manipulate such a large array, and then it is impossible to conduct routing searches in some mobile data terminals, such as smart phones and Personal Digital Assistance (PDAs). The comparison between the adjacency matrix and incidence

matrix can give the same result. Assuming an adjacency matrix occupies more storage space than that of an incidence matrix,

then

$$|V|^2 \geq |E| \times |V|$$

From equation 3.2, we obtain,

$$d(G) \leq 2 \quad (3.6)$$

This means that the adjacency matrix representation occupies more space if and only if equation 3.6 holds. Since the minimum degree of transportation network is 2 ($\delta(G) = 2$), then equation 3.6 is invalid. As a result, the adjacency matrix occupies less storage space than that of the incidence matrix. Since the adjacency matrix cannot compete with the adjacency list in terms of storage space (i.e., requires more space), it follows that the incidence matrix will also not be able to compete.

Other than the space trade off, the different data structures also facilitate different operations. It is easy to find all nodes adjacent to a given node in an adjacency list representation by simply reading its adjacency list. With an adjacency matrix, we must scan over an entire row, taking $O(|V|)$ time, since all $|V|$ entries in row v of the matrix must be examined in order to see which links exist. This is inefficient for sparse graphs since the number of outgoing links j may be much less than $|V|$. Although the adjacency matrix is inefficient for sparse graphs, it does have an advantage when checking for the existence of a link $u \rightarrow v$, since this can be completed in $O(1)$ time by simply looking up the array entry $[u; v]$. In contrast, the same operation using an adjacency list data structure requires $O(j)$ time since each of the j links in the node list for u must be examined to see if the target is node v . However, the main operation in a route search is to find the successors of a given node and the main concern is to determine all of its adjacent nodes. The adjacency list is more feasible for this operation.

The above discussions demonstrate that the adjacency list is most suitable for representing a transportation network since it not only reduces the storage space in the main memory, but it also facilitates the routing computation.

Since transportation networks are a specialized type of graph, some fundamental knowledge of graph theory is required. Some basic concepts, such as the definition of a graph, degree of a graph, and the definition of a path, were introduced at the beginning of this chapter. In the discussion of the degree of a graph, the dense graph and sparse graph have been defined and used in data model discussion. In the data model discussion, three types of data models for graph representation were given: the incidence matrix, adjacency matrix and adjacency list.

The discussion includes a description of each model, an analysis of the space complexity, storage space requirements and an examination of suitable operations for each model. Based on the discussion, an adjacency list is regarded as the best representation of the transportation network considering its own characteristics. My research, will utilize an adjacency list to construct topology of the experimental road network in order to implement my routing computations.

3.3 TYPICAL ROUTING QUERIES

There are various types of routing queries that may be submitted to the centralized GIS server. To answer the queries, many algorithms have been developed to satisfy the conditions and requirements of these queries. The research for generalizing this document is focused on two typical routing queries. The first query deals with finding the optimal route from the current location to a known destination. The other query allows users to locate the closest facility of a certain category (hotel, hospital, gas station, etc.), in terms of travel distance (time), without knowing the destination explicitly.

3.3.1 ROUTING QUERY FOR KNOWN DESTINATION

For this query, the mobile client or driver has a definite destination in mind and desires to acquire the optimal route leading to the destination. Since the traffic condition changes continually over time, the optimal route will change during travel whenever up-to-date traffic conditions are provided. For example, when we want to drive from the airport to the KMA office, we can plan the entire optimal route prior to departure according to the current condition of the transportation network. However, it may not be the final optimal route due to frequent changes in the traffic conditions. So, we have to modify our route midway and plan a new path from the current location to the destination based on real-time traffic conditions. This case is more complicated than the conventional dynamic concept because both the traffic conditions and the query point (location of the driver) are dynamic. This type of query is also defined as an en route query since it is submitted while the client is moving.

3.3.2 ROUTING QUERY FOR UNKNOWN DESTINATION

For this query, drivers may inquire about the location of the closest facility, such as the nearest hotel, hospital or gas station, without knowing the destination in advance. In this case, the closest facility is defined in terms of travel distance (time) within the road network as opposed to travel distance. This query can be classified as the Nearest Neighbor problem.

Both the closest destination and an associated optimal route need to be found based on travel time within the road network. Similarly, the optimal route also has to be recalculated whenever up-to-date traffic conditions are provided. In extreme circumstances, the closest destination may also change. For example, in an unknown city, we may want to find the location of the closest post office after we check into a hotel. From the query result, we are aware of the position and optimal route to the closest post office. In this case, we expect the navigation service not only to provide the adaptive route leading to it, but also to confirm the validity of the closest post office while traveling. If the traffic conditions do not change significantly, the optimal route may only need to be slightly modified. If the traffic conditions change considerably or there are serious traffic congestions around the anticipated post office destination, this post office may no longer be the closest one in terms of traveling time. A new post office location and optimal route must then be determined dynamically based on the current location and traffic conditions. In this scenario, the query is an en route query. To solve this problem, a dynamic nearest neighbor and route searching algorithm is required.

3.4 INTRODUCTION TO THE SHORTEST PATH ALGORITHMS

The shortest path (SP) algorithms are among fundamental network analysis problems. Since 1957 a considerable progress has been made in the SP algorithms after Minty published his paper (1957). Minty succinctly described the basic SP problem for symmetrical networks (a network is symmetrical if for every pair of nodes the cost of a link between the two nodes is independent of their starting node). To state the problem beyond doubt, he suggested constructing a model of the given network. The model is made of strings, each string of the length proportional to the costs of the modelled link.

Finally, to find the links of the SP one has to pull the source node and the destination node of the journey as far away as possible. The tight strings are the links of the SP. Since 1957 there has been a number of major papers published, the most important were published by Bellman (1959), Dijkstra (1959) and Moore (1959). These articles were formative and most of the traffic research has used their results (for example Clercq (1972) and Cooke and Halsey (1966)). These articles are now included in references by most other publications.

There are a number of review papers. One of the utmost importance has been published by Dreyfus (1969). The review gives a comprehensive summary of the research, which has been carried out up to 1969. The article surveys over ten years of research, discussing the most crucial stages and pointing out the wrong and inefficient solutions. The paper also gives a brief solution of the SP problem for time varying costs of links, Which is the basis of this

report. The shortest path algorithms are currently widely used. They are the basis of the network flow problems, tree problems and many related other problems. They determine the smallest cost of travel, of a production cycle, the shortest path in an electric circuit or the most reliable path. In the book by Ahuja ,(1993) one can realize that the SP problem is an underlying problem of the network optimization and that it is closely related to network flows or tree building issues. Internet is a large field where the shortest path algorithms can be applied. The Internet problems involve data packages transmission with the minimal time or by the most reliable path. An example of the SP algorithms in the Internet is given by Cai, (1997). This paper proposes three SP algorithms. The devised algorithms are well explained. The article is closely related to the problem. The same algorithms can be used without fundamental changes to the urban traffic issues. The use of the proposed algorithms for public transportation networks will be studied in the section ‘Shortest path and the environment issues’. Algorithms to be discussed here have a thirty-year old history and solutions to the fundamental problems are well known. The contemporary research is directed toward parallel computing as the method for further lowering of the time complexity bound of the shortest path algorithms. The report is not interested in the parallel approach. The article by Klein and Subramanian (1997) is an example of the shortest path parallel algorithm.

3.5 SOME NETWORK DEFINITIONS

TYPES OF NETWORKS

There are several types of networks of special interest to the project: sparse, planar and road networks. Other types of networks (as grid or dense) are not taken into account.

3.5.1 SPARSE NETWORKS

Sparse networks are those which have the number of links only a few times bigger than the number of nodes. A network of one hundred (100) nodes and four hundred (400) links would be considered sparse but a network with one hundred (100) nodes and five thousand (5000) links would be classified as dense.

Public transportation networks are sparse. From node approximately four links leave. If a sparse network was presented in a matrix form, then in each row of the matrix about only four places would be used, the rest would be left idle. For matrix network representation there are algorithms, which handle efficiently the sparse networks. However, it is recommended

not to use matrix-based algorithms since the matrix representation of a sparse network is highly inefficient. Instead of the matrix algorithms the tree building algorithms can be used as they store the sparse network information in an efficient way (usually using lists). In this thesis, the Dijkstra algorithm which is a basic tree building algorithm has been used. The matrix in figure 1.3 is an example of the inefficient matrix representation of a sparse network since there are more places unused than used.

3.5.2 PLANAR NETWORKS

There are a number of SP algorithms for planar graphs. Methods characteristic to planar graphs (as separators) lower the computational bound of the SP algorithms. Since the road network and transport network are mostly planar, application of the algorithms from this group could bring more efficient solutions to our problem. However, not all road networks are planar, there are viaducts and bridges, which can destroy planarity and thus unable, limit or complicate the application of these algorithms. For this reason the methods for the planar graphs will not be considered. The article by Monika R. Henzinger et al., (1997) proposes three new algorithms for planar graphs.

3.6 ROAD NETWORKS

In the representation of a road network a link represents a road and a node represents a crossroad. The ratio of the number of links to the number of nodes is approximately 3. (Steenbrink, year 1958), gives an example of a road network with about 2000 nodes and 6000 links). The link costs are always non-negative. The road networks are usually planar and sparse. The number of nodes is big, usually expressed in thousands. Road networks contain loops, which are allowed since they may be only of a non-negative cost (the link costs are only non-negative). The road networks are of a special interest in this thesis. The characteristic feature of the road networks is their nonnegative link lengths property. Dijkstra year made a good use of nonnegative lengths to design his algorithm. Because of this close relation between Dijkstra, algorithm and road characteristic, it should not be surprising that this report suffers constant 'Dijkstra' referring. The project's road network of the Kumasi City had about seven hundred and eighteen (718) nodes and one thousand one hundred and eighty – seven (1187) links. The network represents the link connections between nodes and the distances between them.

3.7 A GENERAL CLASSIFICATION OF THE ALGORITHMS

The Shortest Path algorithms are either matrix algorithms or tree building algorithms (tree algorithms are also called labelling algorithms).

3.7.1 MATRIX ALGORITHMS

Matrix algorithms store the network information in the matrix form and carry out the computations using basic matrix operations (as addition and multiplication of matrices or matrix's elements). In dense networks is for all pair problems. The disadvantage of the matrix algorithms is the imposed matrix representation. The first disadvantage is the imposed inefficient matrix representation of a sparse network. The more significant disadvantage is that the matrix representation allows one directed link between two nodes (there can be at most two links between two nodes, but they have to be of distinct directions).

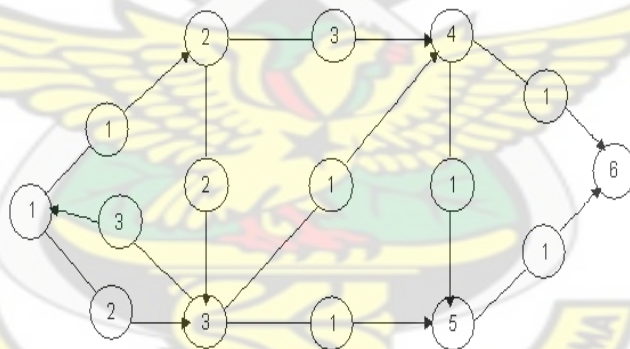


Figure 3.2 : A sample network that can be represented in a matrix form

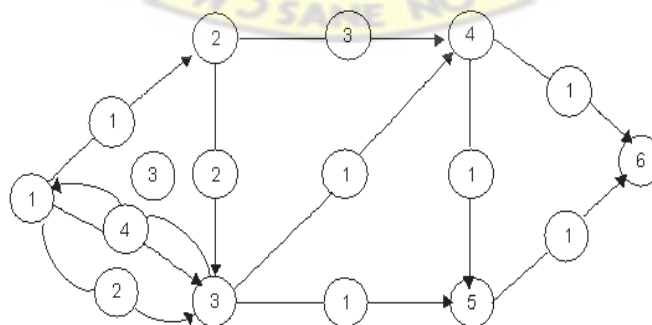


Figure 3.3: A sample network that can be not represented in a matrix form

$$M = \begin{pmatrix} 0 & 1 & 2 & \infty & \infty & \infty \\ \infty & 0 & 2 & 3 & \infty & \infty \\ 3 & \infty & 0 & 1 & 1 & \infty \\ \infty & \infty & \infty & 0 & 1 & 1 \\ \infty & \infty & \infty & \infty & 0 & 1 \\ \infty & \infty & \infty & \infty & \infty & 0 \end{pmatrix}$$

Figure 3.4: Matrix representation of the network of Figure 3.1

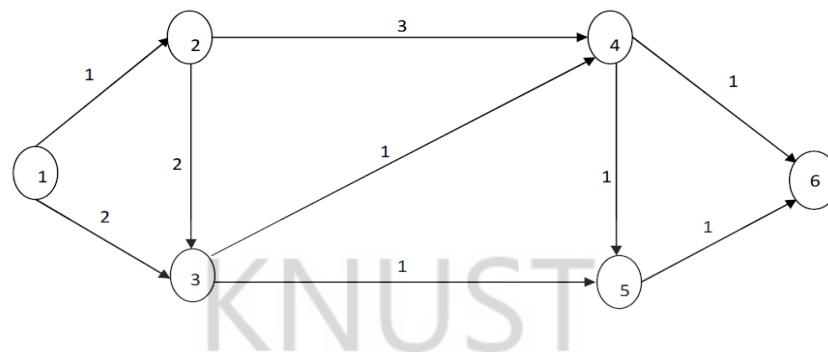
The network from Figure 3.1 is specified by a matrix in Figure 3.4. Not every network can be represented in such a way. If a network has more than one directed link from a single node to some other node, then it cannot be represented in a regular matrix since it can store only one directed link going from a specific link to some other node. A sample network capable of being represented as a matrix is depicted in Figure 3.1. The network has two links connecting the 1st node to the 3rd node. The link from the 1st node to the 3rd node is ascribed the cost of, which is stored in the M matrix in Figure 3.4. As $a_{13} = 2$. The link which goes in the reverse direction (from the 3rd node to the 1st node) is ascribed the cost of 3, this is stored as $a_{31} = 3$. If there was a need to represent the three links between the 1st and 3rd nodes from the Figure 3.4 then we realise we have run out of places in the matrix and the network cannot be fully represented by a matrix. There can be some improvements of the matrix representation envisaged for coping with such an extended network. One improvement is a matrix of lists. An entry in this matrix of lists would not characterise only one directed link from one node to another but a list of directed links from this node to another node. However, this is not classified anymore as the matrix approach to the SP problem because computations of most matrix algorithms would not be performed anymore using basic matrix operations.

3.7.2 THE TREE BUILDING ALGORITHMS

The thesis algorithms are tree building algorithms. A tree building algorithm builds a tree with the root in the source node of the trip. Each node of the network can be either a leaf or a fork of the tree. A fork leads to another forks or leaves. There are certain true statements about the tree. The first is that there are p leaves then these leaves are p nodes of the biggest cost to reach among all nodes. The second says that each fork node (a node that is a fork in the tree) is of the cost smaller than a cost of any leaf node (a node that is a leaf in the tree). Building such a tree is a dynamic programming task since the result of a node just reached can be used to calculate the cost of the node which can be reached immediately after

this node. An example of building a tree for a simple network is presented in the Figure 1.4. To build this tree we use the Dijkstra algorithm.

a) Network



b) Tree

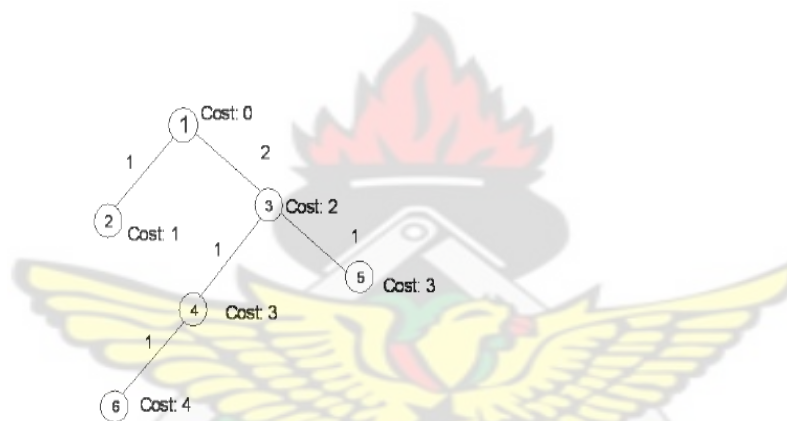


Figure 3. 5: A network and its shortest path tree.

3.8 THE INPUT AND THE OUTPUT TO THE SHORTEST PATH ALGORITHMS

Depending where we are and where we want to go an algorithm can find as many SP's as it is necessary to satisfy us. The SP algorithms can be divided into groups that differ by the given input and the desired output. The groups are: one pair algorithms, one to many, many to one, and all pairs algorithms.

3.8.1 ONE PAIR

There are two nodes given: the source node and the destination node. A SP algorithm finds only one SP (if it exists) from the given source node to the given destination node. The tree algorithms are going to build an incomplete tree with the root in the source node. The tree will be complete up to the moment the destination node has been reached. The Dijkstra algorithm (1959) and the Bellman (1958) algorithm are examples are one pair algorithms.

3.8.2 ONE-- TO -- MANY

Only the source node is specified. All shortest paths from this source node to all other nodes will be calculated. If there is a path from the source node to every other node, then there will be $(n-1)$ SP's evaluated (n is the number of nodes in the network). A tree building algorithm will create a complete shortest path tree. The Dijkstra algorithm and the Bellman algorithm are also examples of one to many algorithms.

3.8.3 MANY – TO- ONE

This problem is given many source nodes and one destination node. To each source node there is time ascribed saying what time the journey starts from this node. The solution to the problem is to find the shortest path from any source node to the destination node that will result in reaching the destination node at the minimal time of arrival (not cost of the journey). This type of a problem is easy to solve having the Dijkstra algorithm. The solution doesn't differ significantly from the Dijkstra algorithm. Only at the beginning one has to put all the source nodes into the priority queue with appropriate costs.

3.8.4 ALL PAIRS

For this algorithm group there is neither a necessity for source node nor for the destination node. An algorithm from this group calculates all the possible $n^2 - n = n(n - 1)$ SP's, i.e. the algorithm is to find the shortest path for every pair of nodes. The number of paths is therefore (the paths from one and the same node is 0 and doesn't require calculation). The computations are mostly done on matrices. The Floyd algorithm (1962) is an example from the all pairs algorithm group.

The project makes use of 'one to many' algorithm and 'many to one' algorithm only. The 'all pairs' algorithm is not essential for the project and will not be discussed.

3.9 ALL – PAIRS SHORTEST PATH PROBLEM

The shortest path between two nodes might not be a direct edge between them, but instead involve a detour through other nodes. The all- pairs shortest path problem requires that we determine shortest path distances between every pair of nodes in a network.

Shortest path problems are the most fundamental and the most commonly encountered problem in the study of transportation and communication networks (syslo et al., 1983).

There are many types of shortest-path problem. For example, we may be interested in determining the shortest path (i.e., the most economical path or fastest path, or minimum-fuel-consumption path) from one specified node in the network to another specified node; or we may need to find shortest paths from a specified node to all other nodes. Shortest paths between all pairs of nodes in a network are required in some problems. Sometimes, one wishes to find the shortest path from one given node to another given node that passes through certain specified intermediate nodes.

In some application, one requires not only the shortest path but also the second and third shortest path. There are instances when the actual shortest path is not required, but only the shortest distance is required.

Next, we shall confine ourselves to two most important shortest-path problems; How to determine shortest distance (a short path) from a specified node to another specified node t , and ~how to determine shortest distances (all paths) from every node to every other in the network. Shortest path route problem deals with determining the connected arcs In a transportation network that collectively comprise the shortest distance.

Between a source and a destination. The shortest path problem involves a weighted, possibly directed graph described by the set of edges and vertices shortest path deals with two algorithms for finding the shortest route.

SHORTEST PATH PROBLEMS

The computation of shortest paths has been extensively researched since it is a fundamental issue in the analysis of transportation networks. There are many factors associated with shortest path algorithms. First, there is the type of graph on which an algorithm works - directed or undirected, real-valued or integer link costs, and possibly negative or non-negative link-costs. Furthermore, there is the family of graphs on which an algorithm works - acyclic, planar, and connected. All of the shortest path algorithms presented in this thesis assume directed graphs with non-negative real-valued link costs.

3.10 CLASSIFICATION OF SHORTEST PATH (SP) PROBLEMS

Even though different researchers tend to group the types of shortest path problems in slightly different ways, one can discern, in general, between shortest paths that are calculated as one-to-one, one-to-all, or all-to-all. Given a graph, one may need to find the shortest paths from a single starting node v to all other nodes in the graph. This is known as the single-source shortest path problem.

As a result, all of the shortest paths from v to all other nodes form a shortest path tree covering every node in the graph. Another problem is to find all of the shortest paths between all pairs of nodes in the graph. This is known as the all-pairs shortest path problem. One way to solve the all-pairs shortest path problem is by solving the single source shortest path problem from all possible source nodes in the graph. Dijkstra's

algorithm is an efficient approach to solving the single-source shortest path problem on positively weighted directed graphs with real-valued link costs. Many of today's shortest path algorithms are based on Dijkstra's approach. There is also the relatively simple single-pair shortest path problem, where the shortest path between a starting node and a destination node

must be determined. In the worst case, this kind of problem is as difficult to solve as single-source.

3.11 CLASSICAL SHORTEST PATH ALGORITHMS FOR STATIC NETWORKS

Path finding is applicable to many kinds of networks, such as roads, utilities, water, electricity, telecommunications and computer networks, the total number of algorithms that have been developed over the years is immense, depending only on the type of network involved. Labeling algorithms are the most popular and efficient algorithms for solving the SP problem. These algorithms utilize a label for each node that corresponds to the tentative shortest path length p_k to that node. The algorithm proceeds in such away that these labels are updated until the shortest path is found.

Labeling algorithms can be divided into two sets: the label setting (LS) algorithms and label correcting (LC) algorithms. For each number of iteration, the LS algorithm permanently sets the label of a node as the actual shortest path from itself to the start node, thus increasing the shortest path vector by one component at each step. The LC algorithm does not permanently set any labels. All of the components of the shortest path vector are obtained simultaneously; a label is set to an estimate of the shortest path from a given at each iteration. Once the algorithm terminates, a predecessor label is stored for each node, which represents the previous node in the shortest path to the current node. As a result, it only determines the path set, $P_k = \{p_1, \dots, p_k\}$, in the last step of the algorithm. Backtracking is then used to construct the shortest paths to each node. Typical label setting algorithms include Dijkstra's algorithm and the A* algorithm. The Floyd-Warshall algorithm is an example of a label correcting algorithms.

3.12 FLOYD WARSHALL ALGORITHM

The Floyd –Warshall algorithm obtains a matrix of shortest path distances within $O(n^3)$ computations. The algorithm is based on inductive arguments developed by an application of a dynamic programming technique. Let $d^k(I, j)$ represent the length of the shortest path from node I to node j subject to the condition that this path uses the nodes $1, 2, \dots, k - 1$ as internal nodes. Clearly, $d^{k+1}(I, j)$ for all node pairs I and j , when it terminates. Given $d^k(I, j)$, the algorithm computes d^{k+1} (using $d^{k+1}(I, j) = \min_k \{d^k(I, k) + d^k(k, j)\}$). The Floyd Warshall algorithm remains of interest because it handles negative weight edges correctly (Ahuja et al., 1993). Floyd Warshall algorithm or Floyd's algorithm is also known as the **all** pairs shortest path algorithm. It will compute the shortest path between all possible pairs of vertices in a (possibly weighted) graph or digraph **simultaneously** in time $O(n^3)$ (where n is the number of vertices in the graph) In this problem we want the minimum routes (m.r.) between all the pairs of peaks. As an example of a path problem, the fire-brigade keeps a map of the city marked with the locations of especially hazardous sites, such as chemical stores. They wish to know the shortest route from the fire-station to each site. Note the "length" of a road might be either its physical length or the estimated driving time on it, which are not necessarily proportional to each other. The Floyd algorithm solves this problem. This algorithm is an expansion of another algorithm, the Warshall algorithm, which was first defined for the solution of another problem:

In a digraph G (whether there are costs or not, is of no importance) find whether there is a route from $V(i)$ to $V(j)$, for all pairs of (i, j) , $i < j$. To solve this problem we find an array A . The elements of this array are $A(i, j) = 1$ if there is a route from i to j otherwise $A(i, j) = 0$. Because the cost is not important we define the Adjoining Array as if all the costs were 1 that means $C(i, j) = 1$ if there is e_{ij} belonging to E and otherwise $C(i, j) = 0$. The requested array A is called transitive closure of the Adjoining Array.

We notice that the elements of the A array are Boolean variables (0 or 1), which means that the operations AND and OR are valid. The Warshall algorithm initializes the A array at the value of C: $A(i,j) = C(i,j)$, $i, j = 1, \dots, n$. At this point the A array shows only the direct connections as existing routes. Then the algorithm goes through the A array n times, one time for every node $k=1 \dots n$. For every node $V(k)$ the main thinking is: Is there a route from $V(i)$ to $V(j)$, if it has already been found [that is $A(i,j)=1$] **or** if a route is found through $V(k)$, that is if the routes from $V(i)$ to $V(k)$ and from $V(k)$ to $V(j)$ [that is if $A(i,k)=1$ and $A(k,j) = 1$].

If the BOOLEAN characteristics of the elements of A are taken under consideration, then the rule in the k pass is: $A(i,j) = A(i,j) \text{ OR } \{A(i,k) \text{ AND } A(k,j)\}$.

We now come back to the m.r. problem for all pairs. This time we are talking about a graph, and the Adjoining Array is defined by the costs $C(i,j)=c(e_{ij})$. The A array will finally consist of all the costs of the minimum routes. During the k pass the following formula is valid: $A(i,j) = \min\{A(i,j), A(i,k)+A(k,j)\}$. Which means that if the route through $V(k)$ is cheaper will be the winner. That gives us the Floyd algorithm. The complexity of the Floyd Algorithm is (in the worst case): $O(n^3)$. The weight of an edge in a directed graph is often thought of as its length. The length of a path $\langle v_0, v_1, \dots, v_n \rangle$ is the sum of the lengths of all component edges $\langle v_i, v_{i+1} \rangle$. Finding the shortest paths between vertices in a graph is an important class of problem. Single Source Shortest Paths in a Directed Graph.

It turns out that it is as easy to find the shortest paths from a single source to all other vertices as it is to find the shortest path between any two vertices. Usually the source is taken to be v_1 . Dijkstra's algorithm solves this single-source shortest paths problem in $O(|V|^2)$ time. It operates by enlarging the set of vertices 'done' for which the shortest paths from the source are known. Initially done contain just the source v_1 . At an intermediate stage, the vertex not in the set done that is closest to the source is found and added to done. This allows our knowledge of the shortest paths to the remaining vertices in $V - \text{done}$ to be updated. This is repeated until done contain all vertices.

The algorithm follows what is known as a greedy strategy. It adds vertices to done as cheaply as possible. The strategy is often a good heuristic; in this problem it also gives a correct algorithm. As given, the algorithm calculates the lengths of the shortest paths from the source to each other vertex. If it is necessary to find the paths themselves, note that the algorithm traces a rooted tree with the source as the root. When the vector of path lengths is updated, if $P(j)$ is reduced by the 'min' then 'closest' can be associated with j in another vector. This allows the paths to be recovered, in a reverse direction.

Floyd's algorithm calculates the costs of the shortest path between each pair of vertices in $O(|V|^3)$ time. It consists of three nested loops. The invariant of the outer loop is the key to the algorithm. At the start of iteration, P holds the optimal path length from v_i to v_j , for each i and j , considering only paths that go direct or via vertices v_n for $n < k$. This is certainly true initially when $k=1$ and P holds only direct paths. At each iteration the next value of k is considered. There may now be a better path possible from v_i to v_j via this new v_k , but note that it will visit v_k at most once. This means it is sufficient to consider paths from v_i to v_k possibly via $\{v_1, \dots, v_{k-1}\}$ and then on from v_k to v_j also possibly via $\{v_1, \dots, v_{k-1}\}$. Thus the Invariant is maintained. Finally P holds optimal path lengths for unrestricted paths.

In simple terms, the Floyd Warshall algorithm obtains a matrix of shortest path distances within $O(n^3)$ computations. The algorithm is based on inductive arguments developed by an application of a dynamic programming technique.

Let $d^k(i,j)$ represent the lengths of the shortest path from i to node j subject to the condition that this path uses the nodes $1, 2, \dots, k-1$ as internal nodes. Clearly, $d^{n+1}(i,j)$ represents the actual shortest path distance from node i to j . The algorithm first computes $d^1(i,j)$ for all node pairs i and j . using $d^1(i,j)$ it then computes $d^2(i,j)$ for all node pairs i and j . It repeats this process until it obtain $d^{n+1}(i,j)$ for all node pairs i and j , when it terminates. Given $d^k(i,j)$, the algorithm computes $d^{k+1}(i,j) = \min\{d^k(i,k), d^k(k,j)\}$. The Floyd Warshall algorithm remains of

interest because it handles negative weight edges correctly (Ahuja et al., 1993) and (Boffey,1982)

3.13 DIJKSTRA'S ALGORITHM

Dijkstra's algorithm, named after its inventor, has been influential in path computation research. It works by visiting nodes in the network starting with the object's start node and then iteratively examining the closest not-yet-examined node. It adds its successors to the set of nodes to be examined and thus divides the graph into two sets: S , the nodes whose shortest path to the start node is known and S' , the nodes whose shortest path to the start node is unknown. Initially, S' contains all of the nodes. Nodes are then moved from S' to S after examination and thus the node set, S , “grows”. At each step of the algorithm, the next node added to S is determined by a priority queue. The queue contains the nodes S' , prioritized by their distance label, which is the cost of the current shortest path to the start node. This distance is also known as the start distance. The node, u , at the top of the priority queue is then examined, added to S , and its out- links are relaxed. If the distance label of u plus the cost of the out- link (u, v) is less than the distance label for v , the estimated distance for node v is updated with this value. The algorithm then loops back and processes the next node at the top of the priority queue. The algorithm terminates when the goal is reached or the priority queue is empty. Dijkstra's algorithm can solve single source SP problems by computing the one-to-all shortest path trees from a source node to all other nodes.

The pseudo-code of Dijkstra's algorithm is described below.

Function Dijkstra (G , $start$)

- 1) $d[start] = 0$
- 2) $S = \emptyset$
- 3) $S' = V \in G$
- 4) while $S' \neq \emptyset$

- 5) do $u = \text{Min}(S')$
- 6) $S = S \cup \{u\}$
- 7) for each link (u, v) outgoing from u
- 8) do if $d[v] > d[u] + w(u, v)$ // Relax (u, v)
- 9) then $d[v] = d[u] + w(u, v)$
- 10) $\text{Previous}[v] = u$

3.14 A* ALGORITHM

It is not feasible to use Dijkstra's algorithm to compute the shortest path from a single start node to a single destination since this algorithm does not apply any heuristics. It searches by expanding out equally in every direction and exploring a too large and unnecessary search area before the goal is found. Dijkstra's algorithm is a version of a BFS and although this algorithm is guaranteed to find the optimal path, it is not extensively applied due to its relatively high computing cost. This has led to the development of heuristic searches. In terms of heuristic searches, the A* algorithm is widely regarded as the most efficient method. The A* algorithm is a heuristic variant of Dijkstra's algorithm, which applies the principle of artificial intelligence. Like Dijkstra's algorithm, the search space is divided into two sets: S , the nodes whose shortest path to the start node is known and S' , the nodes whose shortest path to the start node is unknown. It differs from Dijkstra's algorithm in that it does not only consider the distance between the examined node and the start node, but it also considers the distance between the examined node and the goal node.

In the A* algorithm, $g(n)$ is called the start distance, which represents the cost of the path from the start node to any node n , and $h(n)$ is estimated as the goal distance, which represents the heuristic estimated cost from node n to the goal. Because the path is not yet complete, we cannot actually know this value, and $h(n)$ has to be “guessed”. This is where the heuristic method is applied. In general, a search algorithm is called admissible if it is guaranteed to

always find the shortest path from a start node to a goal node. If the heuristic employed by the A* algorithm never overestimates the cost, or distance, to the goal, it can be shown that the A* algorithm is admissible. The heuristic is called an admissible heuristic since it makes the A* search admissible. If the heuristic estimate is given as zero, this algorithm will perform the same as Dijkstra's algorithm. Although it is often impractical to compute, the best possible heuristic is the actual minimal distance to the goal. An example of a practical admissible heuristic is the straight-line distance from the examined node to the goal in order to estimate how close it is to the goal. The A* algorithm estimates two distances $g(n)$ and $h(n)$ in the search, ranks each node with the equation: $f(n) = g(n) + h(n)$, and always expands the node n that has the lowest $f(n)$. Therefore, A* avoids considering directions with non-favourable results and the search direction can efficiently lead to the goal. In this way, the computation time is reduced. Thus, the A* algorithm is faster than Dijkstra's algorithm for finding the shortest path between single pair nodes. The algorithm is an example of a best-first search

3.15 COMPARISON OF ALGORITHMS BASED ON DISTANCE (TIME) COMPLEXITY

The efficiency of a search algorithm is a critical issue in route planning since it relates to the practicality and effectiveness of the search algorithm. Since a time consuming search algorithm is inapplicable in real world applications, it is necessary to conduct a complexity analysis for different algorithms. The complexity analysis involves two aspects: time and space complexity. Algorithm requirements for time and space are often contradictory with a saving on space often being the result of an increase in processing time, and vice versa. However, advances in computer hardware have made it possible to provide sufficient memory in most computational environments and the main concern is now the time

complexity of the algorithm. In shortest path computation, there are two essential operations: one is the additive computation which gives the start distance of the current node based on previous nodes and the link weight between them; the other is the comparison operation which gives a possible shorter path to the start node. We assume the time cost for these two operations is equivalent. The time complexity is measured by the frequency of the most used operations in the above algorithms. Observing the pseudo-code of Dijkstra's algorithm in section 3.5.1, the main loop from steps 5 to 10 takes the most computational time. In step 5, the algorithm finds the node with a minimum start distance. It requires $|V|$ times comparison at first time, $|V| - 1$ times at second time and so on. Therefore the time complexity of the node search is $|V| + (|V| - 1) + \dots + 1 = O(|V|^2)$. In steps 8 to 10, the algorithm examines all links that are connected to the current node for the additive and comparison operations. From the view of the entire search, it will examine all of the links in the network, which takes $|E|$ time. Therefore the final time complexity of Dijkstra's algorithm is $O(|V|^2 + |E|) = O(|V|^2)$. For the A* algorithm, its time complexity is calculated in a different way since it only computes the shortest path between a single pair of nodes. If the average degree of a network is denoted as d , and the search depth (i.e., the levels traversed in searching the tree until the goal is found) is denoted as h , then the time complexity of the A* algorithm is $O(dh)$. The time complexity comparison between these two algorithms is shown in Table 3.1.

	Dijkstra's Algorithm	A* Algorithm
Time Complexity	$O(V ^2)$	$O(d^h)$

Table 3.1 Time Complexity Comparison between Classical Algorithms

In this section, I suggest that the shortest path from the current location to a known destination is a typical query for navigation services. Based on the above time complexity comparison, A* is an efficient algorithm to solve the SP problem, because d and h are much

smaller than $|V|$. Thus, the distance (time) complexity of the Dijkstra algorithms is far greater than A* in that they involve redundant computation for solving the single pair SP problem. Since they are more applicable to other shortest path problems, they may be employed in other discussed later in the thesis. Although A* can answer the first type of query proposed in section 1.4, it is not the optimal solution as it is a static approach. In a dynamic environment, A* has to recompute the shortest path from scratch every time there is a change in traffic conditions. From this point of view, it must be improved in order to be adaptable to a dynamic environment.

3.16 DYNAMIC TRAFFIC ROUTING

3.16.1 DYNAMIC TRANSPORTATION NETWORK

Time is an essential part of today's world. While long distance travel time seems to be getting shorter each year, daily commuters have to spend more and more time just getting to their offices. A major reason for this situation is traffic congestion, which results from high traffic flow, incidents, events or road construction. Traffic congestion is perhaps the most conspicuous problem in the transportation network and has become a crucial issue that needs immediate attention. In the past, when drivers encountered traffic congestion, they had to queue up and wait until the congestion cleared. Analysts were content with just studying the queuing times and predicting waiting times, without making any attempt to actually solve the problem. Current countermeasures for traffic congestion are oriented toward a "local" optimum, i.e., a point-to-point diversion by using sign boards to divert traffic flow around the point of congestion. The emergence of LBS gives a new paradigm for applying GIS to transportation issues. As a key component, navigation services are regarded as the most promising solution for solving this problem.

In transportation network representations, the weight of the links can be assigned as the cost of travel time, along the links. Changes in traffic conditions are considered as changes in link-weights, where the congestion occurs. Since traffic conditions always change over time, the centralized navigation service has to monitor the traffic fluctuations over a day-long interval and detect any congestion upstream in order to allow drivers to take preventive action. By using dynamic shortest path algorithms, navigation services can also help mobile clients to plan an alternative optimal route to their destination based on the updated traffic conditions. In this sense, the solution provided by the navigation service is closer to a "global" optimum. This feature also encourages the possibility of deploying these algorithms in real-time traffic routing software.

3.16.2 RELATED RESEARCH FOR DYNAMIC TRAFFIC ROUTING

Recent developments in LBS reflect a propensity for increased use of dynamic algorithms for routing. Most of these algorithms have already been applied successfully for routing in computer networks. As well, these algorithms can be applied to transportation network management, especially in the context of the centralized architecture of navigation services, where traffic flow would exhibit a behaviour close to that of "packets" in computer networks. Motivated by theoretical as well as practical applications, many studies have examined the dynamic maintenance of shortest paths in networks with positive link weights, aiming at bridging the gap between theoretical algorithm results and their implementation and practical evaluation. In dynamic transportation networks, weight changes can be classified as either deterministic or stochastic time-dependent. In the deterministic time-dependent shortest path (TDSP) problem, the link-weight functions are deterministically dependent on arrival times at the tail node of the link, i.e., with a probability of one. In the stochastic TDSP problem, the link-weight is a time-dependent random variable and is modelled using probability density functions and time-dependency. Here, link weights take on time-dependent values based on

finite probability values. Cooke and Halsey first proposed a TDSP algorithm in 1958. The algorithm they suggested is a modified form of Bellman's label correcting the shortest path algorithm. Hall worked on the stochastic TDSP problem and showed that one cannot simply set each link-weight random variable to its expected value at each time interval and solve an equivalent TDSP problem. Frank derived a closed form solution for the probability distribution function of the minimum path travel time through a stochastic time-variant network. There were also a number of other works addressing similar problems. All of these are based on the model of a time dependent network where link length or link travel time is dependent on the time interval. All of the research discussed above attempts to use probabilistic and statistical approaches to determine the random change of link-weights and then derive the most promising shortest path. To simplify the dynamic shortest path (DSP) problem, my thesis research assumes that the link-weight changes are collected and updated by a centralized navigation service. Based on the given link-weights for each time interval, my research focuses on the DSP algorithm itself. The DSP algorithm utilizes current traffic conditions to dynamically maintain the optimal path en route. With a single weight change, usually only a small portion of the graph is affected. For this reason, it is sensible to avoid computing the shortest path from scratch, but only to update the portion of the graph that is affected by the link-weight change. Incremental search methods are used to solve dynamic shortest path problems, where shortest paths have to be determined repeatedly as the topology of a graph or its link costs change. A number of incremental search methods have been suggested in the literature for algorithm, which differ in their assumptions: whether they solve single source or all-pairs shortest path problems; which performance measure they use, when they update the shortest paths; which kinds of graph topology and link costs they apply to; and how the graph topology and link costs are allowed to change over time. An algorithm is referred to as fully-dynamic if both the weight increment and decrement are supported and semi-dynamic if only the weight increment (or decrement) is supported.

Among the algorithms proposed for the DSP problem, the algorithm of Ramalingam and Reps (RR for short, also referred to as the Dynamic SWSF-FX algorithm) seems to be the most used. It is a fully-dynamic DSP algorithm which updates the shortest paths incrementally. In their work on algorithms for the DSP problem. Proposed a fully dynamic algorithm, which is a specialization of the RR algorithm for updating a shortest path tree. It is a modification of their previous work on a semi-dynamic incremental algorithm. This chapter shows that the RR algorithm is an efficient approach for solving the DSP problem. One of its main advantages is that the algorithm performs efficiently in most situations. First of all, it updates a shortest path graph instead of a shortest path tree, although it can be easily specialized for updating a tree. Even and Shiloach proposed a semi-dynamic incremental algorithm that works in cascades, which can be computationally expensive for large link-weight increments. RR has good performance independent of weight increments. For updating a shortest path tree, Demetrescu's semidynamic incremental algorithm performs well only if most of the affected nodes have no alternative shortest paths. However, the RR algorithm performs well even when there are alternative paths available. Even the algorithm of Frigioni et al., (1996) which is theoretically better than RR, was usually outperformed by RR in computational testing. Many theoretical studies of DSP algorithms have been carried out but few experimental results are known. Frigioni et al., (1998) compared the RR algorithm with the algorithm proposed by Frigioni et al., for updating a single-source shortest path graph. They concluded that the RR algorithm is usually better in practice, with respect to running times, but their algorithm has a better worst case time complexity. In this chapter, the shortest path problem is well discussed. The chapter started with the classification of the shortest path problem, which divided the shortest paths into one-to-one, one-to-all, or all-to-all. Commonly used search strategies, such as the breadth-first, depth-first and best-first searches, were then introduced. Based on the search strategy analysis, two classical shortest path algorithms are described as typical solutions to the shortest path problems defined by the

classification. They are Dijkstra's and the A* algorithms, which are devised for static environments. Although the time complexity comparison demonstrates that the A* algorithm is most suitable for calculating the shortest path between single pair nodes due to its static property. The algorithm is inefficient in dynamic transportation networks. To satisfy the requirement of applications for real-world traffic networks, the dynamic shortest path (DSP) problem is addressed. Firstly, the scenario of the dynamic traffic network is provided to illustrate the past and present solutions in the real-world and demonstrate the importance of DSP research. Secondly, some related research on the time-dependent shortest path (TDSP) problem is briefly introduced in order to identify the research area in this thesis, which assumes the link-weight changes have been given. Based on this assumption, some previous algorithms are explored. Among them, the RR algorithm is shown to be the efficient approach in most dynamic environments. It plays a major role in my solution to the DSP problem. Nevertheless, all of the dynamic approaches discussed in this chapter are still not capable of answering the first query type proposed at the beginning of this thesis, i.e., trying to find the adaptive route from the current location to a known destination. These algorithms can only calculate the dynamic shortest path between fixed start and goal nodes for different time intervals. This means that they are not able to deal with changes in the position of the start node as a mobile user moves along the initial optimal path and makes an en route query for a new shortest path in accordance with traffic condition changes.

3.17 SHORTEST PATH AND THE ENVIRONMENT ISSUES

Suppose there is a need to find a path, which implies the smallest usage of fuel. This case is similar as the money cost of the travel, but it differs since the bus money cost (the money for a bus ticket, for example) is higher than (and not linear to) the fuel used. The shortest path in terms of used fuel needs to be evaluated from the environment point of view. The simplest approach to the problem is to ascribe a cost to every link costs that express the impact on the

environment. A higher cost will be attached to a car link, and a smaller cost will be attached to the bus link. The cost of a link should be dependent on the length of a link. According to the criteria of cost, the algorithm searches for the shortest path and at the same time computes the time cost. The time cost of a shortest path generated with the help of such an algorithm will not be optimised. We can conceive the case where there is the shortest path found in terms of the lowest fuel cost, but the time cost is not acceptable. This may happen if we waited a long time to save not a significant amount of fuel.

A number of constraining criteria for such a shortest route finding can be given. First, we can fix a certain amount of time which can be taken at most for waiting at a bus stop. Among the links that fulfil this condition, the link of the smallest fuel cost is chosen. Another constraint can be that the overall travel time cannot be greater than a fixed amount T . In the article by Cai et al., (1997) one can find three algorithms for the internet data packages routing among, which one algorithm is very well suited to our needs. The algorithm searches a specific type of networks. Each link in the network has two numbers ascribed: cost and time. For us the cost can be the fuel cost and time is the time cost. The proposed algorithm is going to find the shortest route according to fuel cost and with the overall time cost not exceeding a specific amount of time T . The main ideas of the project are involved in the adaptation of the algorithm proposed by Dreyfus (1969) for bus networks which is based on the Dijkstra's algorithm. The main ideas have been used to adopt the algorithm described by Dreyfus (1969) to the public transportation networks, to describe it mathematically.

3.18 INTRODUCTION TO THE BUS ROUTING ALGORITHM DESCRIPTION

The algorithm can be used for any public transportation network based on timetables. In any public transports means that the project takes into account, the root for the public transport which must be based on timetables in which the driver reports the bus routing algorithm.

3.18.1 THE BUS ROUTING ALGORITHM

To understand the problem clearly, it is useful to visualise a traveller who wants to get from one bus stop to another in a city using buses only. The input data to the algorithm consists of a description of the bus transportation network (timetables, description of connections between bus stops), the bus stop where the journey begins (the source node) and the bus stop at which the journey ends (the destination node). The objective is to find the shortest path between the two specified nodes, namely the path that requires the minimal amount of time. The algorithm presented here was designed to solve the problem described above. The new algorithm had to be designed in order to meet the special needs of bus transportation networks such as timetables and the possibility of waiting at bus stops. The main difference between the standard shortest path problem and this one is that links vary with distance (time) and it is allowed to wait at the nodes as long as it is necessary to obtain the minimal time cost. The problem can be classified as the shortest path problem with time dependent costs of links and the allowance of waiting at nodes. A time cost of every link may differ in any desired way. The solution to the problem is based on Dijkstra's algorithm, which is the best known algorithm for directed networks with nonnegative link costs. There are several principles (as the use of a priority queue or the use of buckets) underlying an efficient implementation of the Dijkstra algorithm which can also be applied to implement the bus algorithm (the article by Cherkassy et al is a good paper discussing principles for Dijkstra algorithm implementation). The Dijkstra algorithm has to be modified because of two problems:

- (i) The first modification deals with a problem of fixed times at which a bus leaves the bus stop. This new attribute of a link is going to be named the departure time of a link. Dijkstra's algorithm is not concerned with a departure time of a link; the algorithm was designed to work with links, which can be used at any time. In our

problem the main constraint is that links cannot be used at any time, the time at which a bus link can be used is fixed according to a timetable.

(ii) The second problem is the actual cost of a bus connection between two nodes. In our case the cost of a link is not the criterion to judge the optimality of the link choice anymore. In the present problem the actual criterion is the sum of the waiting time and the link cost, or, in other words, the time of arrival at the finishing node of a link. In effect, we are also concerned with the waiting times at nodes. The need to wait at bus stops is a consequence of the departure time attribute (if a link cannot be used right now then it is necessary to wait for the departure). Suppose there are buses leaving a specific bus stop at 1, 2... 10 time units and arriving at the other specific bus stop after the time cost. The time costs of the buses differ considerably since the buses may be of different companies and they may take different routes. Having the data, the task is to find the cheapest connection between two nodes. The task then is to find the link that has the minimum sum of the time cost of a link and the waiting time (that is necessary to wait for this link). We can phrase the solution to the problem in this way: the sought link is the link of which the arrival time is minimal. This formulation of the solution, i.e. finding the minimal arrival time, is going to be used as opposed to the summation of a waiting time and the time cost (which is the same but complicates the coming formulas).

3.19 THE SHORTEST PATH

Let $P = (s = x_1, x_2, \dots, x = x_r)$ be the shortest path from the source node s to the destination node x . The nodes of the shortest path are such that they result in the minimal arrival time to the x_r node. The time of arrival is given by $T(x_r)$. The subsequent nodes of the shortest path are found by the use of $T(x_i)$ function. To find x_{r-1} we have to find the link which led to x_r with minimal arrival time. Having the link, we have the starting node of the link. This starting

node is the x_{r-1} node of the shortest path. This method has to be repeated until the source node is reached.

Step description of the algorithm

The aim of the algorithm is to minimise $T(x)$ (x is the destination node). To minimise it we first have to minimise $T(x_i)$ for nodes x_i which are at the shortest path from s to x . Before we get to the algorithm description, there are some definitions to be introduced. We classify all the nodes of the graph into three sets, every node can be a member of only one of the following sets:

- i. SPN: the Set of Permanent Nodes is the set of nodes which have been completely processed; the time of reaching these nodes has been computed and will not change.
- ii. SSN: the Set of Scanned Nodes is the set of nodes which have been reached, but have not been completely processed; the time cost of getting to them is known but may change.
- iii. SNRN: the Set of Not Reached Nodes is the set of nodes which have not been reached at all.

3.20 DIJKSTRA'S ALGORITHM

Dijkstra's algorithm, conceived by Dutch computer scientist Edsger Dijkstra in 1959, is a graph search algorithm that solves the single-source shortest path problem for a graph with non negative edge path costs, outputting a shortest path tree. This algorithm is often used in routing. For a given source vertex (node) in the graph, the algorithm finds the path with lowest cost (i.e. the shortest path) between that vertex and every other vertex. It can also be used for finding costs of shortest paths from a single vertex to a single destination vertex by stopping the algorithm once the shortest path to the destination vertex has been determined. For example, if the vertices of the graph represent cities and edge path costs represent driving

distances between pairs of cities connected by a direct road, Dijkstra's algorithm can be used to find the shortest route between one city and all other cities.

ALGORITHM

Let's call the node we are starting with an initial node. Let a distance of a node X be the distance from the initial node to it. Our algorithm will assign some initial distance values and will try to improve them step-by-step:

- i. Assign to every node a distance value. Set it to zero for our initial node and to infinity for all other nodes.
- ii. Mark all nodes as unvisited. Set initial node as current.
- iii. For current node, consider all its unvisited neighbours and calculate their distance (from the initial node). For example, if current node (A) has distance of 6, and an edge connecting it with another node (B) is 2, the distance to B through A will be $6 + 2 = 8$. If this distance is less than the previously recorded distance (infinity in the beginning, zero for the initial node), overwrite the distance.
- iv. When we are done considering all neighbours of the current node, mark it as visited. A visited node will not be checked ever again; its distance recorded now is final and minimal.
- v. Set the unvisited node with the smallest distance (from the initial node) as the next "current node" and continue from step 3.
- vi. When all nodes are visited, algorithm ends.

DESCRIPTION OF THE ALGORITHM

Suppose you create a knotted web of strings, with each knot corresponding to a node, and the strings corresponding to the edges of the web: the length of each string is proportional to the weight of each edge. Now you compress the web into a small pile without making any knots

or tangles in it. You then grab your starting knot and pull straight up. As new knots start to come up with the original, you can measure the straight up-down distance to these knots: this must be the shortest distance from the starting node to the destination node. The acts of "pulling up" and "measuring" must be abstracted for the computer, but the general idea of the algorithm is the same: you have two sets, one of knots that are on the table, and another of knots that are in the air. Every step of the algorithm, you take the closest knot from the table and pull it into the air, and mark it with its length. If any knots are left on the table when you're done, you mark them with the distance infinity. Or, using a street map, suppose you're marking over the streets (tracing the street with a marker) in a certain order, until you have a route marked in from the starting point to the destination. The order is conceptually simple: from all the street intersections of the already marked routes, find the closest unmarked intersection - closest to the starting point (the "greedy" part). It's the whole marked route to the intersection, plus the street to the new, unmarked intersection. Mark that street to that intersection, draw an arrow with the direction, then repeat. Never mark to any intersection twice. When you get to the destination, follow the arrows backwards. There will be only one path back against the arrows, the shortest one.

The Dijkstra's algorithm uses two types of labels: temporary and permanent. Both labels utilized the same format used with the cycles algorithm: namely, $[d, n]$, where d is the shortest distance so far available for a current node, and n is the immediate predecessor node responsible for realizing the distance d . The algorithm starts with the source node carrying the permanent label $[0, -]$. Next we consider all the nodes that can be reached directly from source node and then determine their associated labels. The newly created labels are designated as temporary.

The permanent label is selected from among all current temporary labels as the one having the smallest distance d in the label $[d, n]$ (ties are broken arbitrarily). The process is now

repeated for the last node that has been designated permanent. In such a case, a temporary label of a node may be changed only if the new label yields a smaller distance d .

Let us apply the procedure to the network in figure below. a basic assumption of the algorithm is that all the distances in the network are non-negative.

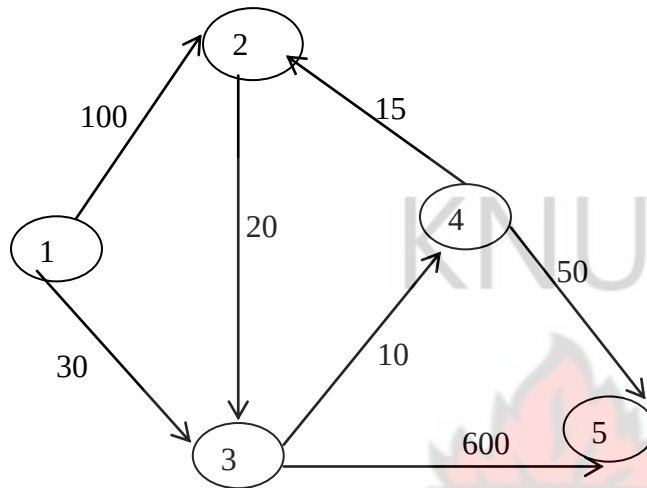


Fig 3.6a : Description of algorithm

Iteration 0: Node 1 carries the permanent label (0)

Iteration 1: Nodes 2 and 3, which can be reached directly from node 1 (the last permanently labeled node), now carry the temporary labels $(0 + 100, 1)$ and $(0 + 30, 1)$ or $(100, 1)$ and $(30, 1)$, respectively. Among the current temporary labels, node 3 has the smallest distance $d + 30$ ($+ \min \{100, 30\}$) thus node 3 is permanently labeled.

Iteration 3: node 4 and 5 can be reached from the last permanently labeled node (node 3) respectively. At this point, we have the three temporary labels $[30 + 10, 3]$ and $[30 + 60, 3]$ (or $[40, 3]$ and $[90, 3]$) associated with nodes 2, 4, and 5, respectively. Temporarily labeled node 4 has the smallest $d = 40$ ($+ \min \{100, 40, 90\}$) and hence its label $[40, 3]$ is converted to the permanently status.

Iteration 3: from the node 4, we now label node 2, with the now temporary label $[40 + 15, 4] = [55, 4]$, which replace the old temporary label $[100, 1]$. Next, node include $[55, 4]$ and $[90, 4]$ associated with nodes 2 and 5, respectively. We thus label node 2 permanently with $[55, 4]$

The only remaining node is the sink node 5, which converts its [90, 4] into a permanent label, thus completing the procedure.

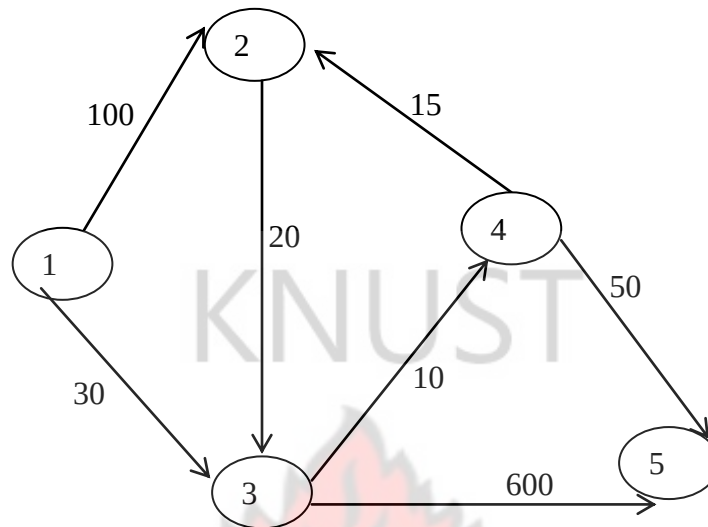


Fig 3.6b: Description of the algorithm

Therefore one would realize that the shortest distance in moving from node 1 to node 2 will be from node 1 (which carries the permanent label (0,1)) through node 3 [30,2] through node 4 [40,3] then finally to node 2 which will have the permanent label [55,4]

The solution in Figure 1.2 provides the shortest distance to each node in the network together with its route. In summary, Dijkstra's algorithm finds the shortest paths from a source node s to all other nodes in a network with non-negative arc lengths. Dijkstra's algorithm maintains a distance label $d(i)$ with each node i , which is an upper bound on the shortest path length from the source node to each node i . At any immediate step, the algorithm divides the nodes of the network under consideration into two groups: those, which it designates as permanently labeled (or permanent), and those, which it designates as temporarily labeled (or temporary). The distance label to any permanent node represents the shortest distance from the source node to that node. The basic idea of the algorithm is to find out from the source node s and permanently label nodes in the order of their distances from the node s . Initially, node s is assigned a permanent label of zero, and each other node j a temporary label equal to infinity. At

each iteration, the label of a node i is the shortest from the source node along a path whose internal node (i.e. node other than s or the node i itself) are all permanently labeled. The algorithm selects a node i with the minimum temporary label (breaking ties arbitrarily), makes it permanent, and reaches out from that node—that is, examines all the edges/arcs emanating from the node i to update the distance labels of adjacent nodes. The algorithm terminates when it has designated all nodes permanent (Ahuja et al, 1993).

THE STEP DESCRIPTION

STEP 1

The source node s is initialised as *scanned* ($s \in SSN$) and every other node $x_i \neq s$ of the graph is initialised as *not reached* ($x_i \in SNRN$). Furthermore, the arrival time of the source node is set to t_0 (t_0 is the time at which the journey starts), i.e. $T(s) = t_0$, and the arrival time of every other node $x_i \neq s$ of the graph is set to infinity, i.e. $T(x_i) = \infty$.

STEP 2

We process only one node during this step. We choose the node to be processed from the SSN (Set of Scanned Nodes). If the SSN is empty, this means there is no path between the source node and the destination nodes and the algorithm quits. If the SSN is not empty, we choose a x_i node from the SSN which has minimal $T(x_i)$. If there is more than one node with the minimal $T(x_i)$ then we choose one of them arbitrarily. In formula:

$$x_i \in SSN \text{ if } T(x_i) = \min_{x_j \in SSN} T(x_j)$$

Once the x_i node is chosen, we proceed to process it. First the node x_i is excluded from the SSN and becomes a member of SPN (Set of Permanent Nodes). At this stage it is certain that the arrival time $T(x_i)$ is minimal (it may only get larger since taking another link will increase the cost; link costs are always positive) and this is the reason for moving the x_i node to SPN.

Next the links leaving the x_i node are handled. From the set E (the set of links of the graph) every link which has the x_i node as a starting one is selected. The retrieved set is further constrained to links of the departure time greater or equal to $T(x_i)$ (only buses that will arrive to a bus stop can be taken, not those which have left).

KNUST



CHAPTER 4

DATA COLLECTION AND ANALYSIS

4.1 DATA COLLECTION

Kumasi is the capital city of the Ashanti Region, a very important and historical Centre for Ghana. It is located about 250 km (by road) northwest of Accra. Kumasi is approximately 300 miles north of the equator and 100 miles north of the Gulf of Guinea. It is the second largest city of Ghana with a population of 1,517,000. The metropolis is made up of 119 sub metros. Currently the emergence service for Kumasi Metropolis can all be located in Adum. Whereas the Ambulance service in the metropolis is located at the Komfo Anokye Teaching Hospital (KATH) and the Fire Service can also be located at Adum near the Kumasi metropolitan office. Cases handled by the Metropolis Ambulance Service (MAS) and Metropolitan Fire Services (MFS) range from Gynaecology, fire and to road accidents.

The MAS and MFS are both housed in a separate building at the KATH polyclinic and KMA and both runs two shifts systems; day and night. Communication is the key to running of these services.

This thesis offers an application solution for dynamic routing of vehicles in Kumasi. It proposes a routing system that users employs historical traffic data to model recurring congestion and compute initial shortest path. As unpredicted (nonrecurring) congestion occurs and is reported from some FM station or traffic control centre, the system analyses the real time data to determine if the planned route needs to be change (modified). It can changed the planned route as a function of the current position, destination location, and real time traffic condition The proposed routing system has been composed of three subsystems including ArcGIS Network Analyst (for the digitized map), Dijkstra's algorithm and VB.Net for the software development. The routing optimization problem in traffic management has

been already explored with a number of algorithms. Routing algorithms use a standard of measurement called a metric (i.e. path length) to determine the optimal route or path to a specified destination. Optimal routes are determined by comparing metrics, and these metrics can differ depending on the design of the routing algorithm used (Parker, 2001).

Different kinds of algorithms have been proposed to finding the optimal routes, such as:

- i. Simulated Annealing is a related global optimization technique which traverses the search space by generating neighbouring solutions of the current solution (Kirkpatrick et al., 1983).
- ii. Tabu Search is similar to Simulated Annealing, in that both traverse the solution space by testing mutations of an individual solution. While simulated annealing generates only one mutated solution, tabu search generates many mutated solutions and moves to the solution with the lowest fitness of those generated (Glover et al., 1997).
- iii. Genetic Algorithms (Holland, 1975) use biological methods such as reproduction, crossover, and mutation to quickly search for solutions to complex problems. Genetic algorithm begins with a random set of possible solutions. In each step, a fixed number of the better current solutions are saved and they are used to the next step to generate new solutions using genetic operators.
- iv. The ant colony optimization algorithm which has been used to produce nearoptimal solutions to the travelling salesman problem. They have an advantage over simulated annealing and genetic algorithm approaches when the graph may change dynamically (Dorigo et al., 1999).
- v. Dijkstra's algorithm, used by Network Analyst, is a greedy algorithm that solves the single-source shortest path problem for a directed graph with nonnegative edge weights (Dijkstra, 1959).

However, Network Analyst is still relatively new software, so there is not much published material concerning its application traffic management. Miller (2005) compares the RouteSmart 4.40, the ArcLogistics Route and the ArcMap Network Analyst extension on the ability of either software package to create routes usable by the Drivers in Adum, efficient manner for the city of Kumasi in Ashanti Region

Dijkstra's Algorithm, introduced in 1959 provides one the most efficient algorithms for solving the shortest-path problem. In a network, it is frequently desired to find the shortest path between two nodes. The weights attached to the edges can be used to represent quantities such as distances, costs or times. In general, if we wish to find the minimum distance from one given node of a network, called the source node or start node, to all the nodes of the network, Dijkstra's algorithm is one of the most efficient techniques to implement. In general, the distance along a path is the sum of the weights of that path. The minimum distance from node **a** to **b** is the minimum of the distance of any path from node **a** to **b**.

4.2 NETWORK DATA ANALYSIS AND RESULTS

ArcGIS Network Analyst is a powerful extension that provides network-based spatial analysis including routing, travel directions, closest facility, and service area analysis. ArcGIS Network Analyst enables users to dynamically model realistic network conditions, including turn restrictions, speed limits, height restrictions, and traffic conditions at different times of the day (ESRI 2006). The users with Network Analyst extension are able to:

- (i). Find efficient travel routes,
- (ii). Determine which facility or vehicle is closest,
- (iii). Generate travel directions, and

- (iv). Find a service area around a site.

In the current work, using Network Analyst, an optimum route for the routine find in particular area is generated in the area under study. Network Analyst uses the Dijkstra's Algorithm (Dijkstra 1959) in order to solve the Routing Problem and it can be generated based on two criteria (Lakshumi et al 2006):

- (i). **Distance criteria:** The route is generated taking only into consideration the location of the waste large items. The volume of traffic in the roads is not considered in this case.
- (ii). **Time criteria:** The total travel time in each road segment should be considered as the: Total travel time in the route = runtime of the vehicle + distance time. The runtime of the vehicle is calculated by considering the length of the road and the speed of the vehicle in each road. The Network Analyst extension allows the user to perform "Find Best Route", which solves a network problem by finding the least cost impedance path on the network from one stop to one or more stops. Network modelling gives the opportunity to the user to include the rules relating to the objects, arcs and events in association with solving transportation problems (Stewart 2004).

4.2.1 THE PATH FINDING ALGORITHM

Network Analyst software determines the best route by using an algorithm which finds the shortest path, developed by Edgar Dijkstra (1959). Dijkstra's algorithm is the simplest path finding algorithm, even though these days a lot of other algorithms have been developed. Dijkstra's algorithm reduces the amount of computational time and power needed to find the optimal path. The algorithm strikes a balance by calculating a path which is close to the optimal path that is computationally manageable (Olivera, 2002). The algorithm breaks the network into nodes (where lines join, start or end) and the paths between such nodes are

represented by lines. In addition, each line has an associated cost representing the cost (length) of each line in order to reach a node. There are many possible paths between the origin and destination, but the path calculated depends on which nodes are visited and in which order. The idea is that, each time the node, to be visited next, is selected after a sequence of comparative iterations, during which, each candidate-node is compared with others in terms of cost (Stewart, 2004).

The following comprehensible example, which is an application of the algorithm on a case of 6 nodes connected by directed lines with assigned costs, explains the number of steps between each of the iteration of the algorithm (Figure 5.1). The shortest path from node 1 to the other nodes can be found by tracing back predecessors (bold arrows), while the path's cost is noted above the node.

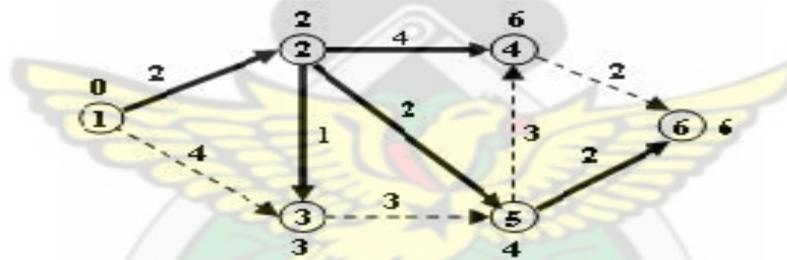


Figure 4:1 An example of Dijkstra's algorithm (Orlin 2003).

Each node is processed exactly once according to an order that is being specified below.

Node 1 (i.e. origin node) is processed first. A record of the nodes that were processed is kept; call it Queue (Table 1). So initially Queue = {1}. When node k is processed the following task is performed: If the path's cost from the origin node to j could be improved including the vertex (k,j) in the path then, an update follows both of Distance[j] with the new cost and Predecessors[j] with k, where j is any of the unprocessed nodes and Distance[] is the path's cost from the origin node to j. The next node to be processed is the one with the minimum Distance [j], in other words is the nearest to the origin node among all the nodes that are yet to be processed. The shortest route is found by tracing back predecessors.

		Distance						Predecessors				
Queue	Next node	1	2	3	4	5	6	2	3	4	5	6
1	2	-	2	4	∞	∞	∞					
1,2	3	-	-	3	6	4	∞		2	2	2	
1,2,3	4	-	-	-	6	4	∞					
1,2,3,5	5	-	-	-	6	-	6					5
1,2,3,5,4	6	-	-	-	-	-	6					
1,2,3,5,4,6	-	-	-	-	-	-	-					

Table 4:1 A record, called Queue, with all processed nodes

Network Analyst can be very useful in a variety of sections (ESRI 2006) in our daily life, such as in:

- i. Business, scheduling deliveries and installations while including time window restrictions, or calculating drive time to determine customer base, taking into account rush hour versus midday traffic volumes.
- ii. Education, generating school bus routes honouring curb approach and no U-turn rules.
- iii. Environmental Health, determining effective routes for county health inspectors.
- iv. Public Safety, routing emergency response crews to incidents, or calculating drive time for first responder planning.
- v. Public Works, determining the optimal route for point-to-point pickups of massive trash items or routing of repair crews.
- vi. Retail, finding the closest store based on a customer's location including the ability to return the closest ranked by distance.
- vii. Transportation, calculating accessibility for mass transit systems by using a complex network dataset.

4.3 CASE STUDY

A digital road network in small area of Kumasi (Adum), capital of Ashanti Region, was used within the GIS map at a scale of about 1:2000. The road network was represented as connections of the nodes and links. Geometric networks are built in the ArcGIS model to construct and maintain topological connectivity for the road data in order to allow the path finding analysis to be possible. To plan the initial shortest path, use historical data of average traffic volume at surface streets or freeway segments within the area under study. The segment lengths have been extracted using ESRI's ArcGIS software. The average volume of each link in the network has been from obtained from KMA Traffic Unit. Summation of the travel distance (times) for all the segment of a particular path between origin and destination provides the total distance (time), which is minimized by the shortest path algorithm. The routing macro uses Dijkstra's routing algorithm.

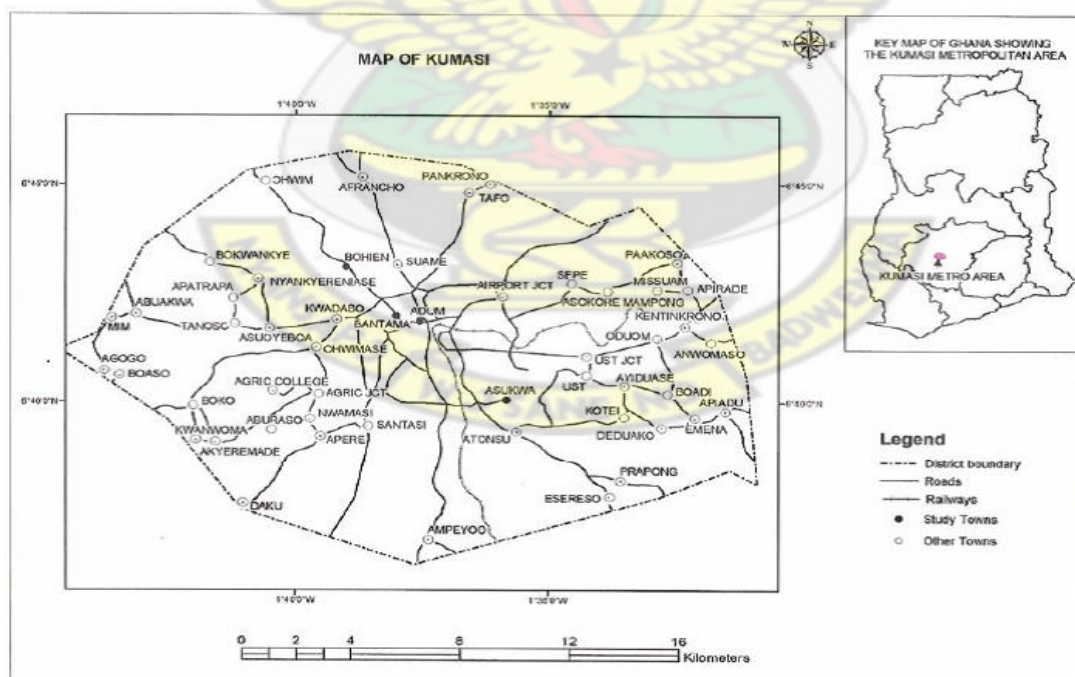


Fig 4.2 map of Kumasi metropolis

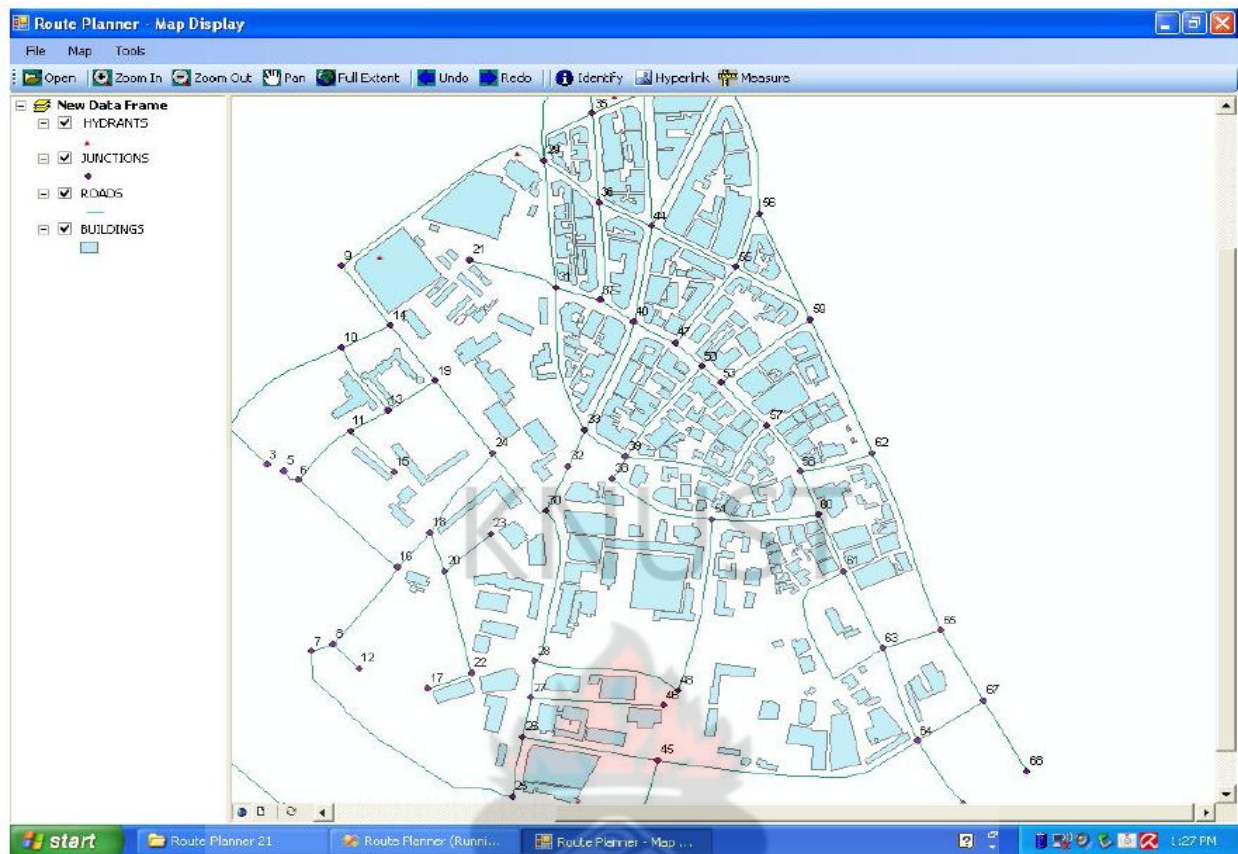


Figure 4:3 Shows the map of Adum.

4.4 PROPOSED SOLUTION

This thesis describes a study of planning vehicle routes for the shortest path in a district of Adum using Network Analyst - a user-friendly extension of ArcGIS and Visual Basis Dot Net with Dijkstra's algorithm, which provides efficient routing solutions in a simple and straightforward manner. In order to simulate the situation in ArcGIS, all the relevant information was acquired from KMA. More precisely, when creating a network routing solution, specific spatial data are needed for the accurate completion of the network. For example, a complete road network, where all the roads within the network are connected, is significant because it allows connection throughout the system.

MODEL ASSUMPTIONS

- Traffic congestion not considered
- Calculation based on road distance
- State of the road not considered

Adum map was taken from the Town and Country Planning Department of KMA.

Digitized by the Geodetic Department (KNUST) to convert the map into a road network

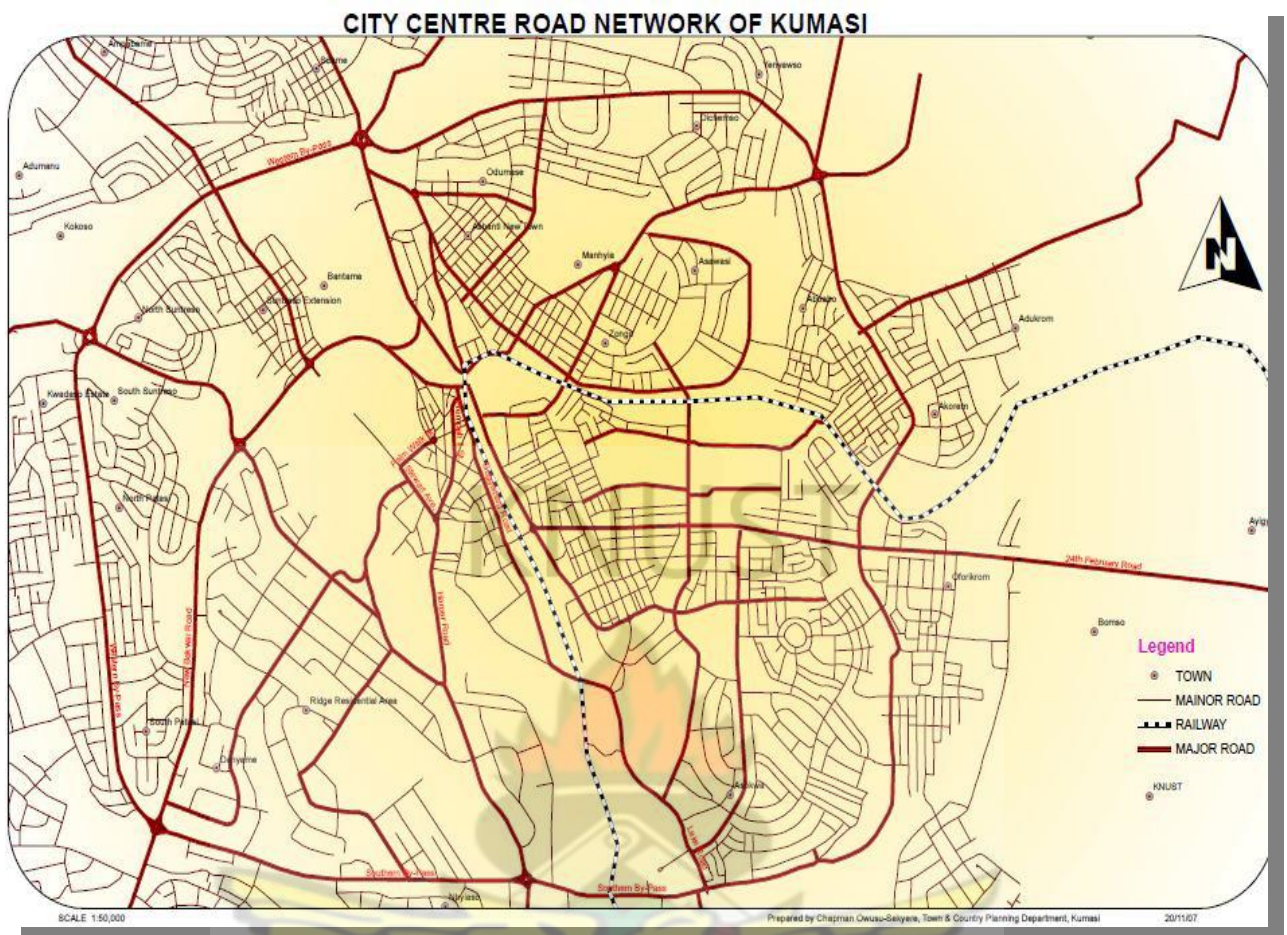


Figure 4.4: Shows the City Centre Road Network of Kumasi

EXTRACT MAP OF ADUM NETWORK

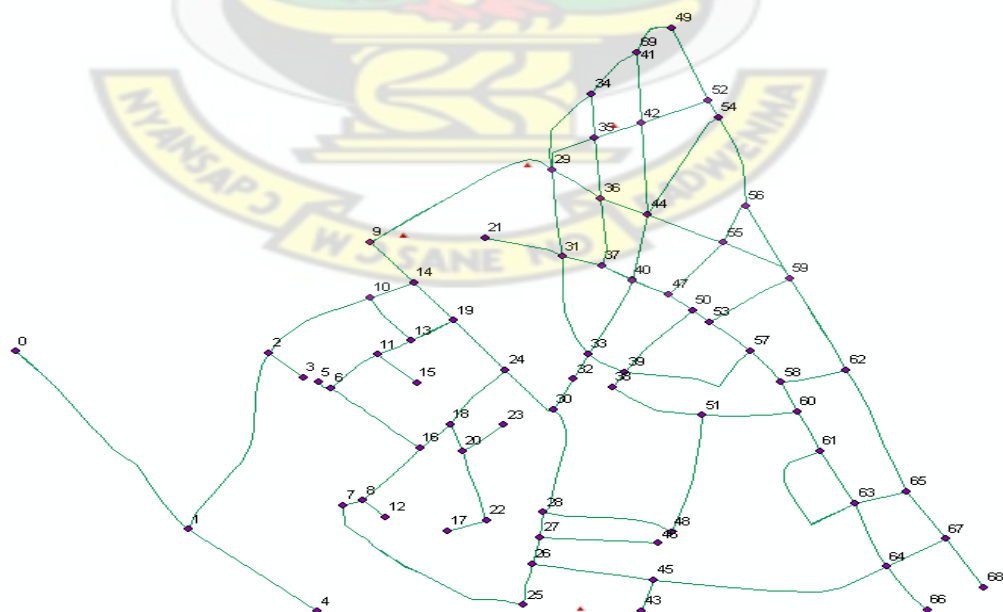


Figure 4.5: Shows the Extract Map of Adum Network

SOFTWARE DEVELOPMENT

The proposed routing system has been of three subsystems including:

- ArcGIS Network Analyst
- Dijkstra's Algorithm
- VB.Net

For the software development

FEATURES OF THE INTERFACE

Step one: The first interface of the program.

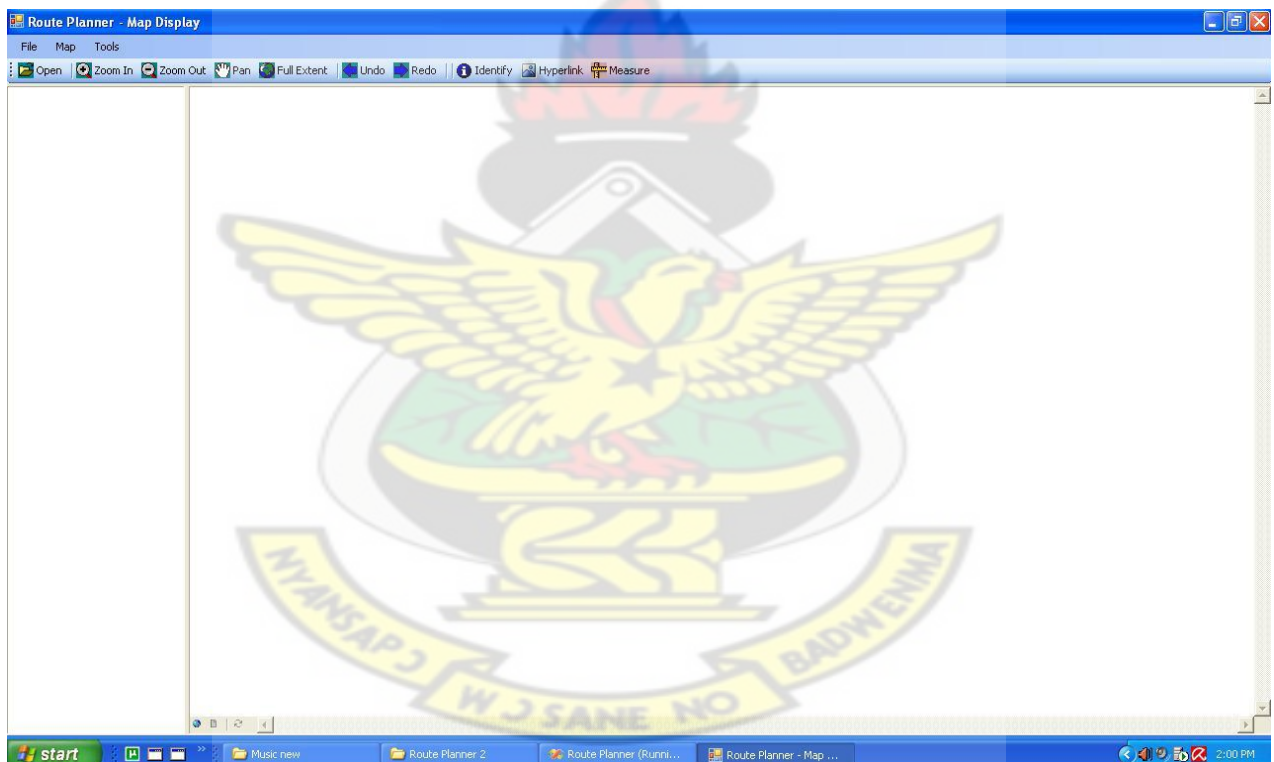


Figure 4.6: Shows the first interface of the program

Step two: The user open to select to select the map needed.

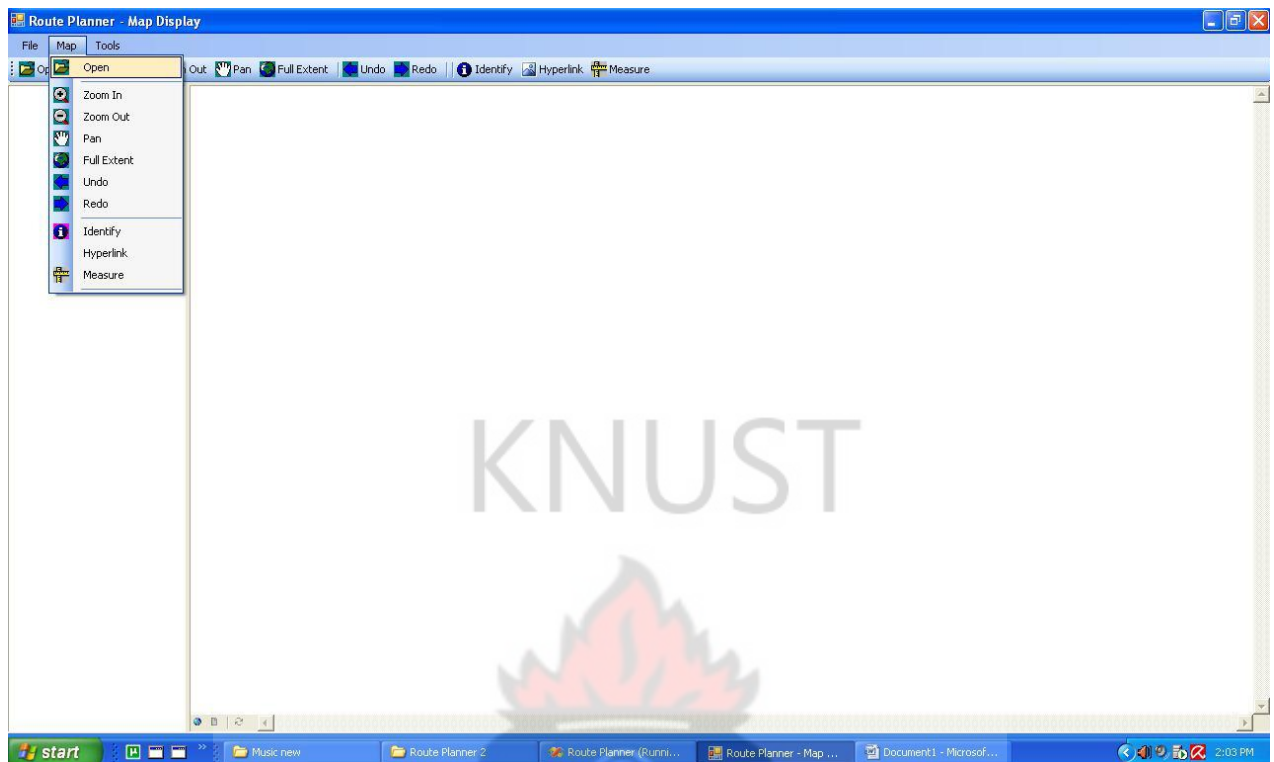


Figure 4.7: Shows the how users select a map

Step Three: The user selects the needed map from the dialogue box to be open.

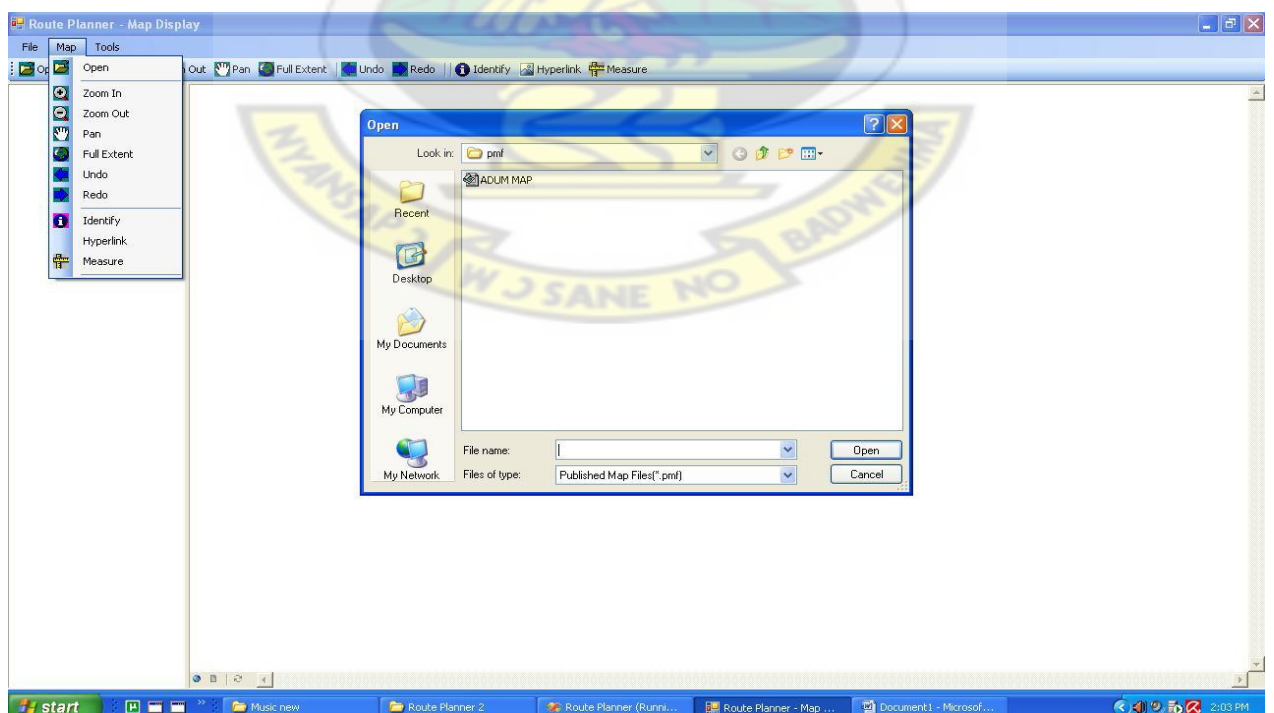


Figure 4.8: Shows how the maps are the display and selected.

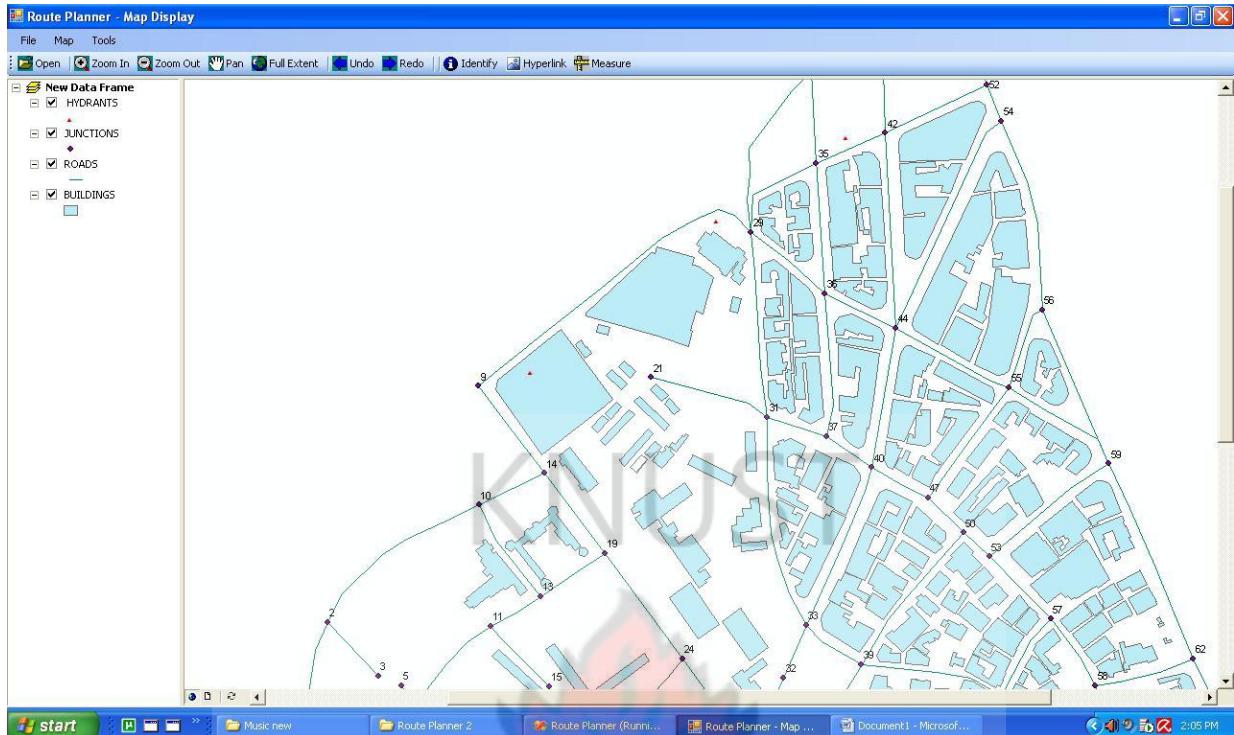


Figure 4.9: Shows how the selected map been displayed

Step Four: The user uses the tool menu to select the Shortest Path Navigator where the user selects the Source Street and the Destination. The flash bottom flashes the selected street and the Flicker also flicks the selected street. The Go button uses to calculate the shortest distance from the Source Street to the Destination Street on the map, and then display the distance on the blank space. The Flash Features shows the shortest path on the map.



Figure 4.10: Shows how the user selects the Source Street and the Destination

Step Five: How the streets are been selected.

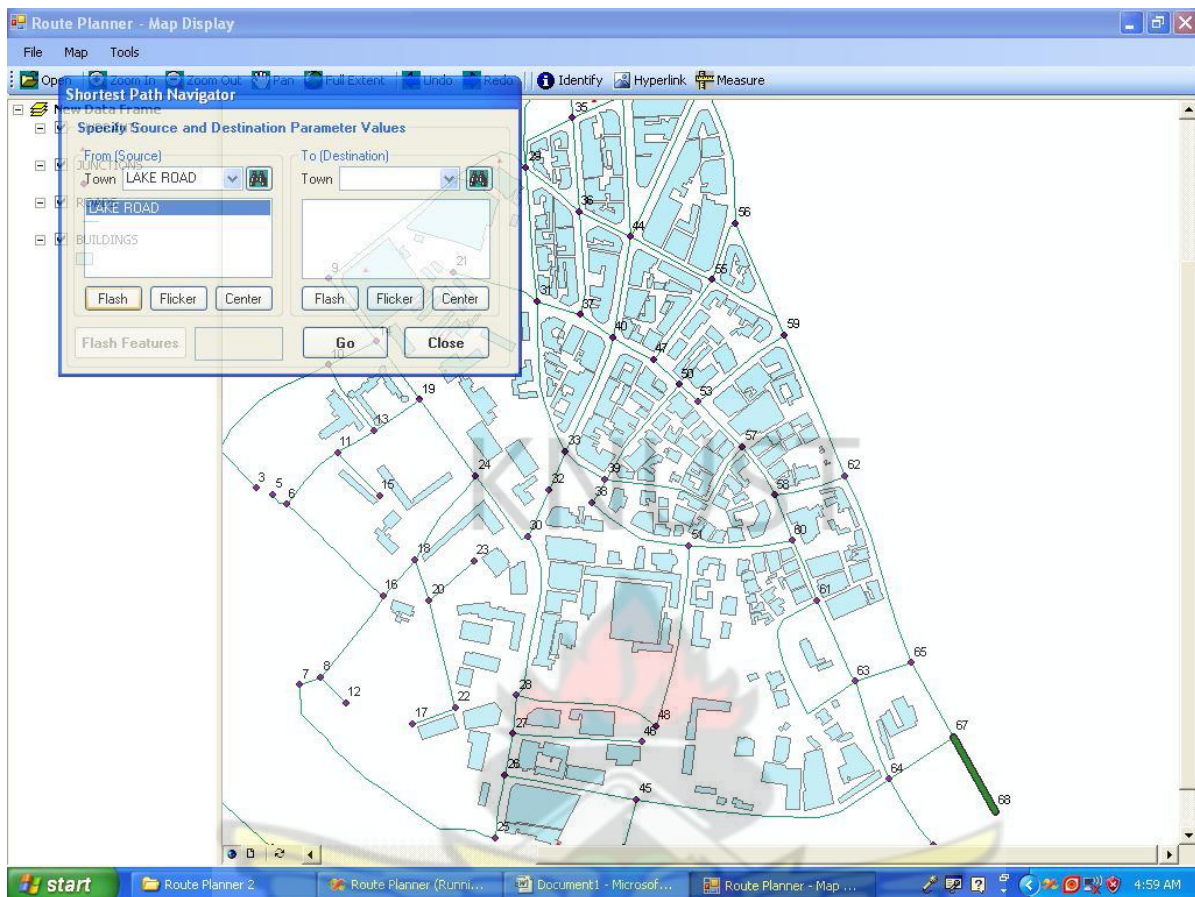


Figure 4.11: Shows how user selects the Source Street.

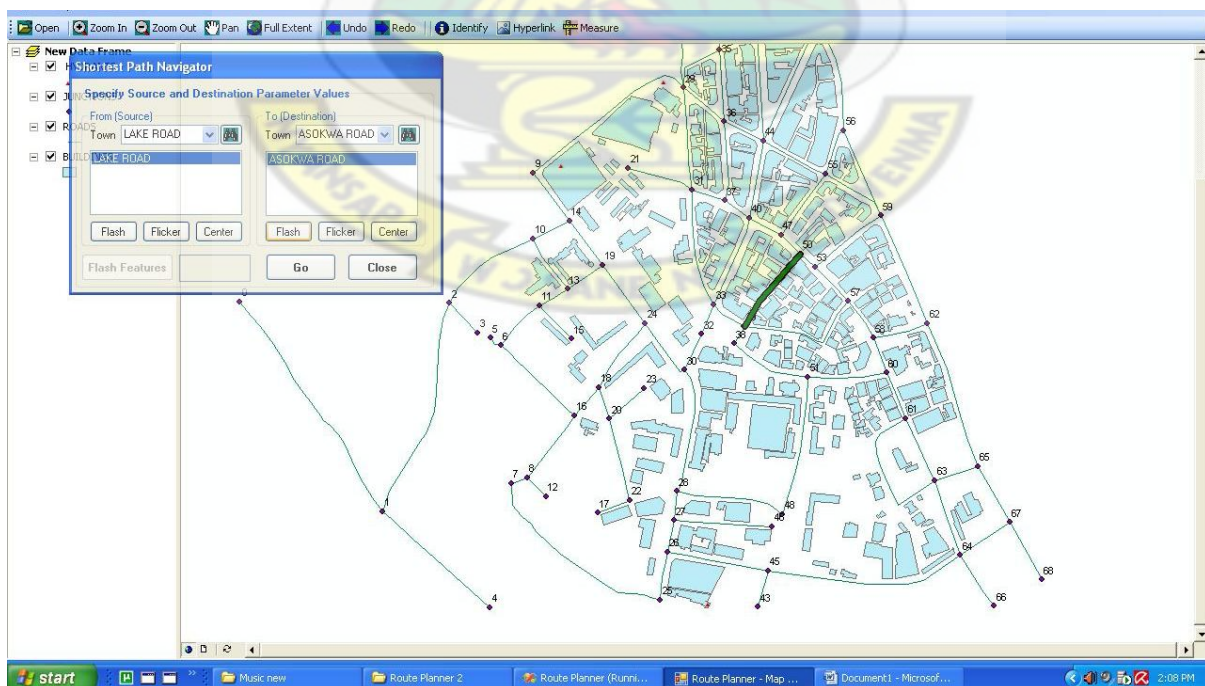


Figure 4.12: Shows how user selects the Destination Street.

4.5 DISCUSSION AND FUTURE WORK

These interfaces show how legend was loaded and displayed for the software obtained. The source node Adum (A) was made fixed and the destination node was to be selected. The program was run after loading the data .The computation was done by the program as:

Adum chosen as the starting node (A) was assigned a permanent label of zero and each other node a temporal label. Each node is labelled with a distance from the start and a previous node. Each node is held in a queue to be evaluated later. The algorithm select a node with minimum temporal label to be evaluated from the queue, makes it permanent and reaches out from that node. All nodes adjacent to this vertex that have been visited were labeled and held in the queue.

The process continues until all the nodes in the queue had permanent label and algorithm terminated. The shortest path to a given node was labelled on that vertex. The path was found by tracking back through the network. The software displayed the source, destination, the shortest path and the optimal distance in kilometres. The result attained is able to provide the shortest distance from Adum to any location. It also provides the routes to obtain the shortest distances. Computation of shortest paths is a famous area of research in Computer Science, Operations Research and GIS. There is a great number of ways to calculate shortest paths depending on the type of network and problem specification. Network Analyst is not only capable of reproducing a satisfying number of scenarios, but also it has the ability to be easily adapted to new conditions.

CHAPTER FIVE

CONCLUSIONS AND RECOMMENDATIONS

5.1 CONCLUSION

In conclusion the shortest distance from any area on Kumasi to another can be calculated, let us have a look at the case of an emergence call, requesting an ambulance to rush a patient from any of the part of Kumasi to a KATH hospital. The shortest distance can easily be known using this project, because a link on a real road network in the city tends to posse different levels of congestion during different time period of a day and because a Patient's location cannot be expected to be known in advance, it is practically impossible to determine the fastest route before a call is received. The collection, transport and disposal of solid waste, which is a highly visible and important municipal service, involves a large expenditure but receives, scant attention. This problem is even more crucial for large cities in developing countries due to the hot weather once again the shortest distance can also be calculated using this project. This study addresses the problem of determining dynamic shortest path in traffic networks, where arc travel times vary over time. This study proposes a dynamic routing system which is based on the integration of GIS and real-time traffic conditions. It uses GIS for improving the visualization of the urban network map and analysis of car routing. GIS is used as a powerful functionality for planning optimal routes based on particular map travel time information. The results of this study illustrate that dynamic routing of emergency vehicle compared with static solution is much more efficient. This efficiency will be most important when unwanted incidents take place in roads and serious traffic congestion occur. In this study, the initial planned route is saved since when exist at any distance. The routing system analysis real distance data receives only portion of the planned path traffic data and

vehicle location to determine if the direction may be a changed. This improves the computational planned route need to be modified.

- This study addresses the problem of determining shortest path in traffic networks, in Kumasi Metropolis
- The study proposes a routing system which is based on the integration of ArcGIS and road distance.
- It uses ArcGIS and VB.NET coding to obtain user friendly interface which allows the visualization of the Adum road map and traversal of shortest route between two selected junctions. The updated route is send via a dynamic routing system for all vehicles in urban (Adum) road communication system to vehicle driver to change his network has some special considerations which are the route. This process continues until the mission of subject of our future work.

5.2 SUGGESSTION

Sometimes the given algorithms may produce output that is of no use even though it has been correctly generated. For example, there can be a path that will require an ambulance and one bus only to reach the destination after 30 minutes. However, the algorithm may advise you to take a car and three times to take a bus which will take 25 minutes, 5 minutes less than the previous path. From the point of view of the defined conditions the second path is better, but a more reasonable path is the first one, though 5 minutes shorter. The first path is actually better because it is less cumbersome (it is easier to take one bus instead of three), more reliable (three buses cause more risk than only one since each bus can break down, changing buses is risky as opposed to sitting in the bus) and is cheaper. This example proves the need to introduce different conditions for solving the shortest route problem. The future research

can go into two directions. First, well known algorithms can be adapted into the public transport needs. For example, the algorithm for finding second shortest path, third etc, paths for buses can be developed. More can be proposed: finding the shortest path going through specific nodes, through specific number of nodes or by the most reliable path.

The other direction is more interesting: development of new algorithms for traffic issues and not just adaptation of existing algorithms. So far there has not been devised (as far as the author of this report knows) an algorithm for many public transport means: a train, an underground, buses and a car. There would not be anything interesting in this except that the buses and metro would be considered in parallel. A user could point out that the path should be build up in accordance with the following criteria:

- The allowed types of changes (for example to change a bus to a train may be disallowed).
- Transportation, calculating accessibility for mass transit systems by using a complex network map.
- Public works, determining the optimal route for point- to – point pickups of trash items.
- Public Safety, routing emergency response crew to incidents, or calculating drive distance for first responder planning. More than that, user can specify exactly how many changes he wants between different types of transportation. For example the user can say that only one change between car and bus is allowed but that changing between buses and an underground vehicle can be done as many times as necessary. Also, the number of changes can be named as *at most* or *exactly*. Therefore saying at most 3 changes of vehicle can ban choosing the best route with only one change. But still, this is should also be possible to find the path with exact number of changes. The flexibility of conditions seems to be very big.

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KNUST



APPENDIX

CODES FOR THE SHORTEST PATH USING VB.NET

```
using System;
using System.Collections;
using System.Collections.Generic;
using System.Text;
using System.Windows.Forms;
using ESRI.ArcGIS.PublisherControls;
using GpsToolsNET;
namespace ShortestPathLibrary
{
    Public# class MapLibrary
    {
        public static int ProgressValue = 0;
        public MapLibrary()
        {
        }
        public static bool LoadMap(AxArcReaderControl arcReaderControl)
        {
            try
            {
                OpenFileDialog ofd = new OpenFileDialog();
                ofd.Filter = "Published Map Files (*.pmf)|*.pmf";
                if (ofd.ShowDialog() == DialogResult.OK)
                {
                    return LoadMap(arcReaderControl, ofd.FileName);
                }
            }
            else
            {
                throw new Exception("");
            }
        }
        catch (Exception ex) { return false; }
    }
    public static bool LoadMap(AxArcReaderControl arcReaderControl,
        string mapPath)
    {
        try
        {
            if (arcReaderControl.CheckDocument(mapPath))
            {
                arcReaderControl.LoadDocument(mapPath);
                return true;
            }
        }
        else
        {
            throw new Exception("");
        }
    }
    catch (Exception ex) { return false; }
    }
    public static void CurrentARTool(AxArcReaderControl
        arcReaderControl, MapTool mapTool)
    {
        try
        {
            if (mapTool == MapTool.FullExtent)
```

```

{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap)
arcReaderControl.ARPageLayout.FocusARMap.ZoomToFullExtent();
else if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypePageLayout)
arcReaderControl.ARPageLayout.ZoomToWholePage();
}
if (mapTool == MapTool.MapHyperlink)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapHyperlink;
}
if (mapTool == MapTool.MapIdentify)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapIdentify;
}
if (mapTool == MapTool.MapIdentifyUsingLayer)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapIdentifyUsingLayer;
}
if (mapTool == MapTool.MapMeasure)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapMeasure;
}
if (mapTool == MapTool.MapSwipe)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapSwipe;
}
if (mapTool == MapTool.MapZoomInOut)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapZoomInOut;
}
if (mapTool == MapTool.Pan)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapPan;
else if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypePageLayout) arcReaderControl.CurrentARTool =
esriARTool.esriARToolLayoutPan;
}
if (mapTool == MapTool.RedoExtent)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap)
arcReaderControl.ARPageLayout.FocusARMap.RedoExtent();
else if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypePageLayout)
arcReaderControl.ARPageLayout.RedoExtent();
}
}

```

```

}
if (mapTool == MapTool.UndoExtent)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap)
arcReaderControl.ARPageLayout.FocusARMap.UndoExtent();
else if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypePageLayout)
arcReaderControl.ARPageLayout.UndoExtent();
}
else if (mapTool == MapTool.ZoomIn)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapZoomIn;
else if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypePageLayout) arcReaderControl.CurrentARTool =
esriARTool.esriARToolLayoutZoomIn;
}
else if (mapTool == MapTool.ZoomOut)
{
if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypeMap) arcReaderControl.CurrentARTool =
esriARTool.esriARToolMapZoomOut;
else if (arcReaderControl.CurrentViewType ==
esriARViewType.esriARViewTypePageLayout) arcReaderControl.CurrentARTool =
esriARTool.esriARToolLayoutZoomOut;
}
}
catch (Exception ex) { }
}
public static MapField GetMapField(ARLayer layer, string
fieldName)
{
try
{
if (layer == null) throw new Exception("");
MapField mapField = new MapField();
ArcReaderSearchDef searchDef = new
ArcReaderSearchDefClass();
ARFeatureCursor featureCursor =
layer.SearchARFeatures(searchDef);
ARFeature feature = featureCursor.NextARFeature();
for (int i = 0; i < feature.FieldCount; i++)
{
if
(feature.get_FieldName(i).Trim().Equals(fieldName.Trim().ToUpper(),
StringComparison.CurrentCultureIgnoreCase))
{
mapField.FieldIndex = i;
mapField.FieldName = feature.get_FieldName(i);
mapField.FieldType = feature.get_FieldType(i);
break;
}
}
}
return mapField;
}
catch (Exception ex) { return null; }
}
public static MapField GetMapField(ARLayer layer, int
fieldIndex)

```

```

{
try
{
if (layer == null) throw new Exception("");
MapField mapField = new MapField();
ArcReaderSearchDef searchDef = new
ArcReaderSearchDefClass();
ARFeatureCursor featureCursor =
layer.SearchARFeatures(searchDef);
ARFeature feature = featureCursor.NextARFeature();
mapField.FieldIndex = fieldIndex;
mapField.FieldName = feature.get_FieldName(fieldIndex);
mapField.FieldType = feature.get_FieldType(fieldIndex);
return mapField;
}
catch (Exception ex) { return null; }
}
public static bool GetShortestPath(NetworkAnalystInitialiser
naInit)
{
try
{
if (naInit.InitialiserStatus.Status)
{
ShortestPathNavigator spNavigator = new
ShortestPathNavigator(naInit);
if (spNavigator.InitialiserStatus.Status)
{
spNavigator.Show(naInit.OwnerForm);
}
else
{
throw new
Exception(spNavigator.InitialiserStatus.Message);
}
}
else
{
throw new
Exception(naInit.InitialiserStatus.Message);
}
return true;
}
catch (Exception ex) { return false; }
}
public static void FlashFeatures(ARFeature[] features, int
millisecondsTimeout)
{
foreach (ARFeature feature in features)
{
feature.Flash();
System.Threading.Thread.Sleep(millisecondsTimeout);
}
}
public static void FlashAndHighlightFeatures(ARFeature[]
features, int millisecondsTimeout)
{
foreach (ARFeature feature in features)
{
feature.Flash();
feature.Highlight(true, 15000);
}
}
}

```



```

System.Threading.Thread.Sleep(milliSecondsTimeout);
}
foreach (ARFeature feature in features)
{
    feature.Highlight(false, 100000);
}
}
public static void FlashAndSelectFeatures(AxArcReaderControl
arcReaderControl, ARFeature[] features, int milliSecondsTimeout)
{
    ARFeatureSet featureSet;
    foreach (ARFeature feature in features)
    {
        feature.Flash();
        System.Threading.Thread.Sleep(milliSecondsTimeout);
    }
}
public static void FlashFeatures(ARFeatureSet features, int
milliSecondsTimeout)
{
    for (int i = 0; i < features.ARFeatureCount; i++)
    {
        features.get_ARFeature(i).Flash();
        System.Threading.Thread.Sleep(milliSecondsTimeout);
    }
}
public static MapShortestPath
GetShortestPath(NetworkAnalystInitialiser naInit, string sourceNode,
string destinationNode)
{
    try
    {
        if (!naInit.InitialiserStatus.Status)
        {
            System.Windows.Forms.MessageBox.Show("Initialiser
status is not set");
            return null;
        }
        MapDijkstra md = new MapDijkstra(naInit, sourceNode,
destinationNode, null, null);
        if (md.Run())
        {
            MapShortestPath msp = new
MapShortestPath(md.ShortestPath, md.PathCost);
            return msp;
        }
        else
        {
            throw new Exception("There was error solving for
shortest path");
        }
    }
    catch (Exception ex) { return null; }
}
public static MapShortestPath
GetShortestPath(NetworkAnalystInitialiser naInit, ARFeature
sourceFeature, ARFeature destinationFeature)
{
    try
    {
        if (!naInit.InitialiserStatus.Status)

```

```

{
    System.Windows.Forms.MessageBox.Show("Initialiser
status is not set");
    return null;
}
MapDijkstra md = new MapDijkstra(naInit,
sourceFeature.get_ValueAsString(naInit.FromNodeIndex),
destinationFeature.get_ValueAsString(naInit.FromNodeIndex),
sourceFeature, destinationFeature);
if (md.Run())
{
    MapShortestPath msp = new
MapShortestPath(md.ShortestPath, md.PathCost);
    return msp;
}
else
{
    throw new Exception("There was error solving for
shortest path");
}
}
catch (Exception ex) { return null; }
}
public static MapShortestPath
GetShortestPath(NetworkAnalystInitialiser naInit, ARFeature
sourceFeature, string destinationNode)
{
    try
    {
        if (!naInit.InitialiserStatus.Status)
        {
            System.Windows.Forms.MessageBox.Show("Initialiser
status is not set");
            return null;
        }
        MapDijkstra md = new MapDijkstra(naInit,
sourceFeature.get_ValueAsString(naInit.FromNodeIndex), destinationNode,
sourceFeature, null);
        if (md.Run())
        {
            MapShortestPath msp = new
MapShortestPath(md.ShortestPath, md.PathCost);
            return msp;
        }
        else
        {
            throw new Exception("There was error solving for
shortest path");
        }
    }
    catch (Exception ex) { return null; }
}
public static MapShortestPath
GetShortestPath(NetworkAnalystInitialiser naInit, string sourceNode,
ARFeature destinationFeature)
{
    try
    {
        if (!naInit.InitialiserStatus.Status)
        {
            System.Windows.Forms.MessageBox.Show("Initialiser

```

```

status is not set");
return null;
}
MapDijkstra md = new MapDijkstra(naInit, sourceNode,
destinationFeature.GetValueAsString(naInit.FromNodeIndex), null,
destinationFeature);
if (md.Run())
{
MapShortestPath msp = new
MapShortestPath(md.ShortestPath, md.PathCost);
return msp;
}
else
{
throw new Exception("There was error solving for
shortest path");
}
}
catch (Exception ex) { return null; }
}
}
public class MapDijkstra
{
private struct Node
{
public string Label;
public double Distance;
public bool Visited;
public Node(string l, double d, bool v)
{
Label = l;
Distance = d;
Visited = v;
}
}
public ARFeatureSet Edges;
private NetworkAnalystInitialiser naInit;
public ArrayList Nodes;
private ArrayList[] pathNodes;
string sourceNodeLabel, destinationNodeLabel;
ARFeature sourceFeature = null, destinationFeature = null;
public System.Collections.ArrayList PathNodes = new
System.Collections.ArrayList();
public ARFeature[] ShortestPath;
public double PathCost = 0;
public MapDijkstra(NetworkAnalystInitialiser naInit, string
sourceNodeLabel, string destinationNodeLabel, ARFeature sourceFeature,
ARFeature destinationFeature)
{
this.naInit = naInit;
this.sourceNodeLabel = sourceNodeLabel;
this.destinationNodeLabel = destinationNodeLabel;
this.sourceFeature = sourceFeature;
this.destinationFeature = destinationFeature;
ArcReaderSearchDef searchDef = new
ArcReaderSearchDefClass();
Edges = naInit.ARRouteLayer.QueryARFeatures(searchDef);
}
private bool UnvisitedNodeExists()
{
try

```

```

{
foreach (Node node in Nodes) if (!node.Visited) return
true;
return false;
}
catch (Exception ex) { return false; }
}
private Node GetMinimumNode(Node node, int currentNodeIndex)
{
Node minNode = new Node(); minNode.Distance = -1;
double length;
Node tNode;
for (int nodeIndex = 0; nodeIndex < Nodes.Count;
nodeIndex++)
{
tNode = (Node)Nodes[nodeIndex];
if (!tNode.Label.Equals(node.Label) && !tNode.Visited)
{
length = GetEdgeLength(node.Label, tNode.Label);
if (length > 0)
{
if (tNode.Distance < 0)
{
tNode.Distance = node.Distance + length;
pathNodes[currentNodeIndex].TrimToSize();
pathNodes[nodeIndex] = new
System.Collections.ArrayList();
foreach (int ni in
pathNodes[currentNodeIndex]) pathNodes[nodeIndex].Add(ni);
pathNodes[nodeIndex].TrimToSize();
}
else if ((node.Distance + length) <
tNode.Distance)
{
tNode.Distance = node.Distance + length;
pathNodes[currentNodeIndex].TrimToSize();
pathNodes[nodeIndex] = new
System.Collections.ArrayList();
foreach (int ni in
pathNodes[currentNodeIndex]) pathNodes[nodeIndex].Add(ni);
pathNodes[nodeIndex].TrimToSize();
}
}
Nodes[nodeIndex] = tNode;
}
}
foreach (Node nd in Nodes)
{
if (!nd.Visited && nd.Distance > 0)
{
if (minNode.Distance < 0)
{
minNode = nd;
}
else if (minNode.Distance > nd.Distance)
{
minNode = nd;
}
}
}
return minNode;
}

```

```

}
private double GetEdgeLength(string start, string stop)
{
    double length = 0;
    ARFeature tf;
    for (int i = 0; i < Edges.ARFeatureCount; i++)
    {
        tf = Edges.get_ARFeature(i);
        if
        ((tf.get_ValueAsString(naInit.FromNodeIndex).Equals(start) &&
        tf.get_ValueAsString(naInit.ToNodeIndex).Equals(stop)) ||
        (tf.get_ValueAsString(naInit.FromNodeIndex).Equals(stop) &&
        tf.get_ValueAsString(naInit.ToNodeIndex).Equals(start)))
        {
            length =
            Convert.ToDouble(tf.get_Value(naInit.ShapeLengthIndex));
            break;
        }
    }
    return length;
}
private ARFeature GetEdge(string start, string stop)
{
    ARFeature tempFeature = null;
    for (int i = 0; i < Edges.ARFeatureCount; i++)
    {
        tempFeature = Edges.get_ARFeature(i);
        if
        ((tempFeature.get_ValueAsString(naInit.FromNodeIndex).Equals(start) &&
        tempFeature.get_ValueAsString(naInit.ToNodeIndex).Equals(stop)) ||
        (tempFeature.get_ValueAsString(naInit.FromNodeIndex).Equals(stop) &&
        tempFeature.get_ValueAsString(naInit.ToNodeIndex).Equals(start)))
        {
            break;
        }
    }
    return tempFeature;
}
private int SetNodes()
{
    int sourceNodeIndex = -1;
    ARFeature tempFeature;
    Nodes = new ArrayList();
    for (int i = 0; i < Edges.ARFeatureCount; i++)
    {
        tempFeature = Edges.get_ARFeature(i);
        Node startNode = new
        Node(tempFeature.get_ValueAsString(naInit.FromNodeIndex).Trim(), -1,
        false);
        Node endNode = new
        Node(tempFeature.get_ValueAsString(naInit.ToNodeIndex).Trim(), -1,
        false);
        if (Nodes.IndexOf(startNode) < 0)
        {
            if (startNode.Label.Equals(sourceNodeLabel) &&
            sourceNodeIndex < 0)
            {
                startNode.Distance = 0;
                sourceNodeIndex = Nodes.Count;
                Nodes.Add(startNode);
            }
        }
    }
}

```



```

else if (!endNode.Label.Equals(sourceNodeLabel))
{
Nodes.Add(startNode);
}
}
if (Nodes.IndexOf(endNode) < 0)
{
if (endNode.Label.Equals(sourceNodeLabel) &&
sourceNodeIndex < 0)
{
endNode.Distance = 0;
sourceNodeIndex = Nodes.Count;
Nodes.Add(endNode);
}
else if (!endNode.Label.Equals(sourceNodeLabel))
{
Nodes.Add(endNode);
}
}
Nodes.TrimToSize();
pathNodes = new System.Collections.ArrayList[Nodes.Count];
return sourceNodeIndex;
}
public bool Run()
{
try
{
if (sourceNodeLabel.Equals(destinationNodeLabel)) throw
new Exception("Source and destination are similar");
int nodeIndex = SetNodes();
if (nodeIndex < 0) throw new Exception("Nodes could not
be set");
Node currentNode = (Node)Nodes[nodeIndex];
pathNodes[nodeIndex] = new
System.Collections.ArrayList();
while (UnvisitedNodeExists())
{
nodeIndex = Nodes.IndexOf(currentNode);
currentNode.Visited = true;
pathNodes[nodeIndex].Add(nodeIndex);
Nodes[nodeIndex] = currentNode;
if (currentNode.Label.Equals(destinationNodeLabel))
break;
currentNode = GetMinimumNode(currentNode,
nodeIndex);
}
//Make sure source and destination features are part of
the collection
ARFeature tempFeature;
if (destinationFeature != null)
{
tempFeature =
GetEdge(((Node)Nodes[(int)pathNodes[nodeIndex][pathNodes[nodeIndex].Cou
nt - 2])).Label,
((Node)Nodes[(int)pathNodes[nodeIndex][pathNodes[nodeIndex].Count -
1])).Label);
if
(destinationFeature.get_ValueAsString(naInit.ObjectIDIndex).Equals(temp
Feature.get_ValueAsString(naInit.ObjectIDIndex)))
{

```

```

destinationFeature = null;
}
}
if (sourceFeature != null)
{
tempFeature =
GetEdge(((Node)Nodes[(int)pathNodes[nodeIndex][0]]).Label,
((Node)Nodes[(int)pathNodes[nodeIndex][1]]).Label);
if
(sourceFeature.getValueAsString(naInit.ObjectIDIndex).Equals(tempFeature.
getValueAsString(naInit.ObjectIDIndex)))
{
sourceFeature = null;
}
}
//Fill Path Nodes arraylist
if (sourceFeature != null && destinationFeature !=
null)
{
ShortestPath = new
ARFeature[pathNodes[nodeIndex].Count - 1 + 2];
ShortestPath[0] = sourceFeature;
ShortestPath[ShortestPath.Length - 1] =
destinationFeature;
for (int i = 0; i < pathNodes[nodeIndex].Count - 1;
i++)
{
ShortestPath[i + 1] =
GetEdge(((Node)Nodes[(int)pathNodes[nodeIndex][i]]).Label,
((Node)Nodes[(int)pathNodes[nodeIndex][i + 1]]).Label);
}
}
else if (sourceFeature != null)
{
ShortestPath = new
ARFeature[pathNodes[nodeIndex].Count - 1 + 1];
ShortestPath[0] = sourceFeature;
for (int i = 0; i < pathNodes[nodeIndex].Count - 1;
i++)
{
ShortestPath[i + 1] =
GetEdge(((Node)Nodes[(int)pathNodes[nodeIndex][i]]).Label,
((Node)Nodes[(int)pathNodes[nodeIndex][i + 1]]).Label);
}
}
else if (destinationFeature != null)
{
ShortestPath = new
ARFeature[pathNodes[nodeIndex].Count - 1 + 1];
ShortestPath[ShortestPath.Length - 1] =
destinationFeature;
for (int i = 0; i < pathNodes[nodeIndex].Count - 1;
i++)
{
ShortestPath[i] =
GetEdge(((Node)Nodes[(int)pathNodes[nodeIndex][i]]).Label,
((Node)Nodes[(int)pathNodes[nodeIndex][i + 1]]).Label);
}
}
else
{

```

```

ShortestPath = new
ARFeature[pathNodes[nodeIndex].Count - 1];
for (int i = 0; i < pathNodes[nodeIndex].Count - 1;
i++)
{
ShortestPath[i] =
GetEdge(((Node)Nodes[(int)pathNodes[nodeIndex][i]]).Label,
((Node)Nodes[(int)pathNodes[nodeIndex][i + 1]]).Label);
}
}
//Calculate Path Cost
PathCost = 0;
foreach (ARFeature feature in ShortestPath) PathCost +=
Convert.ToDouble(feature.get_Value(naInit.ShapeLengthIndex));
return true;
}
catch (Exception ex) { return false; }
}
}
public class NetworkAnalystInitialiser
{
private Form ownerForm;
private AxArcReaderControl arControl;
private string routeLayerName;
private ArrayList mapLayers;
private ARLayer arRouteLayer;
private ArrayList arLayers;
private ArrayList routeLinkers = null;
private string objectIDField, fromNodeField, toNodeField,
shapeLengthField, linkFieldName;
private int objectIDIndex, fromNodeIndex, toNodeIndex,
shapeLengthIndex, linkFieldIndex;
private bool linkFieldNumeric;
private ResultObject initStatus = new ResultObject();
public NetworkAnalystInitialiser(Form ownerForm,
AxArcReaderControl arControl, string routeLayerName)
{
this.ownerForm = ownerForm;
this.arControl = arControl;
this.routeLayerName = routeLayerName;
mapLayers = new ArrayList();
}
public NetworkAnalystInitialiser(Form ownerForm,
AxArcReaderControl arControl, string routeLayerName, string
nodeLayerName, string objectIDField, string fromNodeField, string
toNodeField, string shapeLengthField)
{
this.ownerForm = ownerForm;
this.arControl = arControl;
this.routeLayerName = routeLayerName;
this.objectIDField = objectIDField;
this.fromNodeField = fromNodeField;
this.toNodeField = toNodeField;
this.shapeLengthField = shapeLengthField;
mapLayers = new ArrayList();
Initialise();
}
public Form OwnerForm
{
get { return ownerForm; }
set { ownerForm = value; }
}

```

```

}
public AxArcReaderControl ARControl
{
    get { return arControl; }
    set { arControl = value; }
}
public string RouteLayer { get { return routeLayerName; } }
public ARLayer ARRouteLayer { get { return arRouteLayer; } }
public ArrayList MapLayers { get { return mapLayers; } }
public ArrayList ARLayers
{
    get { return arLayers; }
}
public ArrayList RouteLinkers
{
    get { return routeLinkers; }
}
public string ObjectIDField
{
    get { return objectIDField; }
    set { objectIDField = value; }
}
public string FromNodeField
{
    get { return fromNodeField; }
    set { fromNodeField = value; }
}
public string ToNodeField
{
    get { return toNodeField; }
    set { toNodeField = value; }
}
public string ShapeLengthField
{
    get { return shapeLengthField; }
    set { shapeLengthField = value; }
}
public string LinkFieldName
{
    get { return linkFieldName; }
    set { linkFieldName = value; }
}
public int ObjectIDIndex
{
    get
    {
        if (initStatus.Status) return objectIDIndex;
        else throw new Exception("Object ID Index Not Set");
    }
}
public int FromNodeIndex
{
    get
    {
        if (initStatus.Status) return fromNodeIndex;
        else throw new Exception("From Node Index Not Set");
    }
}
public int ToNodeIndex
{
    get

```

```

{
    if (initStatus.Status) return toNodeIndex;
    else throw new Exception("To Node Index Not Set");
}
}
public int ShapeLengthIndex
{
    get
    {
        if (initStatus.Status) return shapeLengthIndex;
        else throw new Exception("Shape Length Index Not Set");
    }
}
public int LinkFieldIndex
{
    get
    {
        if (initStatus.Status) return linkFieldIndex;
        else throw new Exception("Link Field Index Not Set");
    }
}
public bool LinkFieldNumeric
{
    get { return linkFieldNumeric; }
}
public ResultObject InitialiserStatus
{
    get { return initStatus; }
}
public MapLayer GetMapLayer(string layerName)
{
    if (initStatus.Status)
    {
        foreach (MapLayer mapLayer in mapLayers)
        {
            if
            (mapLayer.LayerName.Trim().Equals(layerName.Trim(),
            StringComparison.CurrentCultureIgnoreCase))
            {
                return mapLayer;
            }
        }
    }
    return null;
}
public ARLayer GetARLayer(string layerName)
{
    if (initStatus.Status)
    {
        foreach (ARLayer arLayer in arLayers)
        {
            if (arLayer.Name.Trim().Equals(layerName.Trim(),
            StringComparison.CurrentCultureIgnoreCase))
            {
                return arLayer;
            }
        }
    }
    return null;
}
public bool AddRouteLinker(RouteLinker routeLinker)

```



```

{
try
{
if (routeLinkers == null) routeLinkers = new
ArrayList();
routeLinkers.Add(routeLinker);
routeLinkers.TrimToSize();
return true;
}
catch (Exception ex) { return false; }
}
public bool AddMapLayer(MapLayer mapLayer)
{
try
{
mapLayers.Add(mapLayer);
return true;
}
catch (Exception ex) { return false; }
}
private bool AddARLayer(ARLayer arLayer)
{
try
{
if (arLayer.Searchable)
{
if (arLayer.IsGroupLayer)
{
for (int i = 0; i < arLayer.ARLayerCount; i++)
{
AddARLayer(arLayer.get_ChildARLayer(i));
}
}
else
{
if (GetMapLayer(arLayer.Name.Trim()) != null)
arLayers.Add(arLayer);
if
(arLayer.Name.Trim().Equals(routeLayerName.Trim(),
StringComparison.CurrentCultureIgnoreCase)) { arRouteLayer = arLayer; }
}
}
return true;
}
catch (Exception ex) { return false; }
}
public bool Initialise()
{
initStatus.Status = true;
initStatus.Message = "Initialiser correctly set";
try
{
if (this.arControl == null)
{
initStatus.Status = false;
initStatus.Message = "ArcReaderControl not set";
}
if (this.routeLayerName.Trim().Length == 0)
{
initStatus.Status = false;
initStatus.Message = "Route layer not set";
}
}
}
}

```

```

}
arLayers = new ArrayList();
arRouteLayer = null;
for (int i = 0; i <
arControl.ARPageLayout.FocusARMap.ARLayerCount; i++)
{
    if
    (!AddARLayer(arControl.ARPageLayout.FocusARMap.get_ARLayer(i)))
    {
        initStatus.Status = false;
        initStatus.Message = "Layer could not be
added";
    }
}
arLayers.TrimToSize();
objectIDIndex = fromNodeIndex = toNodeIndex =
shapeLengthIndex = linkFieldIndex = -1;
ArcReaderSearchDef searchDef = new
ArcReaderSearchDefClass();
ARFeatureCursor featureCursor =
arRouteLayer.SearchARFeatures(searchDef);
ARFeature feature = featureCursor.NextARFeature();
for (int i = 0; i < feature.FieldCount; i++)
{
    if
    (feature.get_FieldName(i).Trim().Equals(objectIDField.Trim(),
StringComparison.CurrentCultureIgnoreCase)) objectIDIndex = i;
    if
    (feature.get_FieldName(i).Trim().Equals(fromNodeField.Trim(),
StringComparison.CurrentCultureIgnoreCase)) fromNodeIndex = i;
    if
    (feature.get_FieldName(i).Trim().Equals(toNodeField.Trim(),
StringComparison.CurrentCultureIgnoreCase)) toNodeIndex = i;
    if
    (feature.get_FieldName(i).Trim().Equals(shapeLengthField.Trim(),
StringComparison.CurrentCultureIgnoreCase)) shapeLengthIndex = i;
    if
    (feature.get_FieldName(i).Trim().Equals(linkFieldName.Trim(),
StringComparison.CurrentCultureIgnoreCase)) { linkFieldIndex = i;
linkFieldNumeric = (feature.get_FieldType(i) ==
esriARFieldType.esriARFieldTypeInteger || feature.get_FieldType(i) ==
esriARFieldType.esriARFieldTypeSmallInteger) ? true : false; }
}
if (objectIDIndex == -1 || fromNodeIndex == -1 ||
toNodeIndex == -1 || shapeLengthIndex == -1 || linkFieldIndex == -1 )
initStatus.Status = false;
}
catch (Exception ex)
{
    initStatus.Status = false;
    initStatus.Message = ex.Message;
}
return initStatus.Status;
}
}
public class MapShortestPath
{
    private ARFeature[] features;
    private double pathCost;
    public MapShortestPath(ARFeature[] features, double pathCost)
    {

```

```

this.pathCost = pathCost;
this.features = features;
}
public ARFeature[] Features
{
    get { return features; }
}
public double PathCost
{
    get { return pathCost; }
}
}
public class ResultObject
{
    private bool status = false;
    private string message = "";
    public ResultObject()
    {
    }
    public bool Status { get { return status; } set { status = value; } }
    public string Message { get { return message; } set { message = value; } }
}
public class MapLayer
{
    private string layerName;
    private ArrayList searchableFields;
    public MapLayer(string layerName)
    {
        this.layerName = layerName;
        searchableFields = new ArrayList();
    }
    public string LayerName
    {
        get { return layerName; }
        set { layerName = value; }
    }
    public ArrayList SearchableFields
    {
        get { return searchableFields; }
    }
    public bool AddSearchableField(string fieldName)
    {
        try
        {
            searchableFields.Add(fieldName);
            searchableFields.TrimToSize();
            return true;
        }
        catch (Exception ex) { return false; }
    }
}
public class MapField
{
    private int fieldIndex;
    private string fieldName;
    private bool isNumeric;
    private esriARFieldType fieldType;
    public MapField()
    {

```

```

}
public int FieldIndex
{
get { return fieldIndex; }
set { fieldIndex = value; }
}
public string FieldName
{
get { return fieldName; }
set { fieldName = value; }
}
public bool IsNumeric
{
get { return isNumeric; }
}
public esriARFieldType FieldType
{
get { return fieldType; }
set
{
fieldType = value;
if (fieldType == esriARFieldType.esriARFieldTypeDouble
|| fieldType == esriARFieldType.esriARFieldTypeInteger || fieldType ==
esriARFieldType.esriARFieldTypeOID || fieldType ==
esriARFieldType.esriARFieldTypeSingle || fieldType ==
esriARFieldType.esriARFieldTypeSmallInteger)
{
isNumeric = true;
}
else
{
isNumeric = false;
}
}
}
public class RouteLinker
{
private string layerName;
private string linkField;
public RouteLinker()
{
}
public RouteLinker(string layerName, string linkField)
{
this.layerName = layerName;
this.linkField = linkField;
}
public string LayerName
{
get { return layerName; }
set { layerName = value; }
}
public string LinkField
{
get { return linkField; }
set { linkField = value; }
}
}
public enum MapTool
{

```

```

Pan,
ZoomIn,
ZoomOut,
MapHyperlink,
MapIdentify,
MapIdentifyUsingLayer,
MapMeasure,
MapSwipe,
MapZoomInOut,
FullExtent,
UndoExtent,
RedoExtent
}
public enum ShortestPathParameterType
{
FeatureToFeature, None
}
}

```

KNUST

